## Object Recognition



Object recognition

- object recognition is a typical goal of image analysis
- object recognition includes
- object identification
recognizing that one object instance is (physically) identical to another object instance
- object classification
assigning an object to one of a set of predetermined classes
- object categorization
assigning an object to an object category (as proposed in biological vision)



## About Model-based Recognition

## "model" = generic description of a class of objects

- explicit representation of object properties (as opposed to decision procedures which incorporate class properties implicitely)
- generic (class-independent) decision procedure
- reusable and incremental model bases
- no strict correspondence with biological vision



## Model-based Object Recognition

How to classify objects based on a generic description.


## 3D Models vs. 2D Models

## 1. Requirement:

Object models must represent invariant class properties
=> 3D models, properties independent of views

## 2. Requirement



Object models must support recognition
=> 2D models, view-dependent properties

Modern approaches to object recognition are typically a compromise of Requirements 1 and 2.
class hammer
is-a aggregat
has-parts part1, part2
is-a part1 cube
is-a part2 cylinder
coaxially-connected part1 part2


## Holistic Models vs. Component Models

## Holistic ("global") models:

- properties refer to complete object
- local disturbances may jeopardize all properties
z.B. area, polar signature, NN classifier



## Component models:

- object model is described by components and relations between components
- properties refer to individual components
- local disturbances affect only local properties

Example of components:

$$
/-1
$$

## 3D Shape Models

Several 3D shape models have been developed for engineering applications:

- 3D space occupancy
- Oct-trees
- CSG ("Constructive Solid Geometry") models
- 3D surface triangulation

In general, pure 3D models are not immediately useful for Computer Vision because they do not support recognition.

In support of recogntion, special 3D models have been developed which include view-related information:

- EGI ("Extended Gaussian Image")
- Generalized cylinders


## 3D Space Occupancy Model



3D shape represented by cube primitives

- useful for highly irregular shapes (e.g. medical domain)
- useful for robotics applications (e.g. collision avoidance)
- interior cubes do not provide information relevant for views
- no explicit surface properties (e.g. surface normals)


## Oct-trees

- hierarchical 3D shape model
- analog to 2D quad-trees
- each cube is recursively decomposed into 8 subcubes
- access via numbering code


Oct-tree for example (right):


## Extended Gaussian Image (EGI)

- 3D shape model based on a surface slope histogram
- extended to provide view-point information for recognition

example of a 3D surface

B.K.P. Horn Robot Vision The MIT Press 1986
entries on
Gaussian sphere

Each entry represents information for a particular 3D slope and viewing direction:

1. quotient of surface area with this slope and total surface area
2. quotient of visible 3D surface area and area of its 2D projection (as viewed from this direction)
3. direction of axis of minimal inertia of 2D projection of visible surface (as viewed from this direction)

## Recognition with EGI Models

Properties of EGIs:

- scale invariant
- rotation of object corresponds to equivalent rotation of EGI
- convex shapes can be uniquely reconstructed In particular: A convex polyhedron can be reconstructed from the set of orientations and associated areas $\left\{\left(0_{1} a_{1}\right)\left(o_{2} a_{2}\right) \ldots\left(o_{N} a_{N}\right)\right\}$
- In general, reconstruction requires an iterative algorithm


## Recognition procedure:

It is assumed that 3D surface normals are determined (e.g. by laser measurements)

- determine direction of axis of minimal inertia
- determine projected surface area
- determine patches of (approximately) constant 3D surface inclination
- constrained search for models which match the measurements


## Illustration of EGI Recognition Procedure

1. Determine direction of axis of minimal inertia => locations on EGI with corresponding entries
2. Determine projected surface area
=> subset of locations determined by 1 )
3. Determine patches of constant 3D surface inclination
=> rotate EGI into viewing direction of 1 ) and 2 ), compare surface area with corresponding entries
4. Constrained search for models which match the measurements => if 1 ) to 3 ) do not match, choose other models


## Discretizing the Surface of a Sphere

For a computer representation of an Extended Gaussian Sphere, the surface of the sphere has to be tessellated into patches of approximately equal size.

geodesic tessellation has undesirable properties

dodecahedron (left) and icosahedron (right) provide tessallations with 12 and 20 cells, respectively

truncated icosahedron (left) provides 12 pentagonal and 20 hexagonal faces, pentakis dodekahedron (right) provides 60 triangular faces

Further refinements can be obtained by triangularization within the cells of a regular or semiregular solid.

## Representing Axial Bodies

Picasso's "Rites of Spring" shows bodies composed of roughly cylindrical and coneshaped pieces.

What representations capture the inherent restrictions of such shapes?

(a)

## Generalized Cylinders

3D surface determined by sweeping a closed curve along a line
ordinary cylinder swept out by a circle along a straight line

generalized cone swept out by an arbitrary planar cross section, varying in size, along a smooth axis (Binford 71)

generalized cylinder swept out by a closed curve at an angle to a curved axis subject to a deformation function


Generalized cones were used in ACRONYM (Brooks et al. 79) to model mainly artificial objects, e.g. airplanes. Under certain conditions, the 3D surface may be reconstructed from the contours of many views.

## Conditions for 3D Reconstruction from Contours

1. Each line of sight touches the body at a single point => we see a "contour generator"
2. Nearby points on the contour in the image are also nearby in 3D (with only few exceptions)

2 distant points projected onto nearby contour points

3. The contour generator is planar
=> hence inflections of the contour in 2D correspond to inflections in 3D

If a surface is smooth and if conditions 1 to 3 hold for all viewing directions in any plane, then the viewed surface is a generalized cone. (Marr 77)


## Relational Models

Relational models describe objects (object classes) based on parts (components ) and relations between the parts

Relational model can be represented as structure with nodes and edges:
Nodes: parts with properties
e.g.


Edges: relations between parts

e.g. - obtuse-angle

- 2cm-distance
- touches
- surrounds
- left-of
- after


## Relations between Components

| unary relation: | property |
| :--- | :--- |
| n-ary relation: | relation, constraint |

Graphical representation
binary relation:

n-ary relation:

"hypergraph"

## Object Recognition by Relational Matching

## Principle:

- construct relational model(s) for object class(es)
- construct relational image description
- compute R-morphism (best partial match) between image and model(s)
- top-down verification with extended model
model




## Compatibility of Relational Structures

Different from graphs, nodes and edges of relational structures may represent entities with rich distinctive descriptions.
Example: nodes = image regions with diverse properties edges $=$ spatial relations

1. Compatibility of nodes

An image node is compatible with a model node, if the properties of the nodes match.
2. Compatibility of edges

An image edge is compatible with a model edge, if the edge types match.

## 3. Compatibility of structures

A relational image description $B$ is compatible with a relational model $M$, if there exists a bijective mapping of nodes of a partial structure $B^{\prime}$ of $B$ onto nodes of a partial structure M' of $M$ such that

- corresponding nodes and edges are compatible
- $M$ is described by $M^{\prime}$ with sufficient completeness


## Example of a Relational Model (1)

shape to be
recognized:
primitive descriptive elements (nodes)

## Example of a Relational Model (2)

relations between primitive descriptive elements (edges)
$\left.\begin{array}{lll} & \begin{array}{l}\ldots \\ d 10 \\ d 12\end{array} & \begin{array}{l}\text { distance } 10 \pm 1 \\ \text { distance } 12 \pm 1 \\ \text { distance } 14 \pm 1\end{array} \\ \ldots & \ldots\end{array}\right]$

## Example of a Relational Model (3)



## Relational Match Using a Compatibility Graph

nodes of compatibility graph = pairs with compatible properties edges of compatibility graph = compatible pairs
cliques in compatibility graph = compatible partial structures


## Finding Maximal Cliques

clique = complete subgraph

Find maximal cliques in a given compatibility graph

Algorithms are available in the literature, e.g.
Bron \& Kerbusch, Finding all Cliques of an Undirected Graph,
Communications of the ACM, Vol. 16, Nr. 9, S. 575-577, 1973.

- Complexity is exponential relative to number of nodes of compatibility graph
- Efficient (suboptimal) solutions based on heuristic search


## Relational Matching with Heuristic Search

Stepwise correspondence search between model nodes $\{A \ldots \mathrm{G}\}$ and


## Case study: Drawing Interpretation

Transforming paper drawings into CAD formats (Pasternak 94)
=> recognition of contours, dimensioning, symmetry lines, surface markings etc.


## Partonomy of Object Parts



## Specification of an Arrow



| NAME: | arrow |
| :--- | :--- |
| KIND-OF: | symbol |
| PARTS: | L1 TYPE line, P1 TYPE polygon |
| TRIGGER: | P1 |
| CONSTRAINTS: | NOT PART L1 P1 |
|  | NEAR P1.0.end L1.start |
|  | ANGLE P1.0.end L1.start [5 30] => ang |
|  | NEAR P1.1.start L1.start |
|  | ANGLE P1.10.start L1.start ang |
|  |  |

## Processing Cycle



## Property Spaces

Representation of graphical objects in multi-dimensional property spaces to allow effective object retrieval and access via their properties

Example:

arrow in 3D property space with endpoint coordinates $x, y$ und orientation o

How to construct property spaces:


- discretization (coarse quantization) of property values
- set-type property space cells to accommodate multiple objects with identical properties
- overlapping value ranges to avoid boundary effects


## Blackboard Architecture

Independent processes communicate Prozesse via a common database ("blackboard")


Recognition process may be structured into processes dedicated to the recognition of individual components

## Analysis of a Machine Drawing

Recognition of dimensioning


## Analysis of an Electrical Circuit

## Recognition of electrical components



## Qualitative Relations

Quantitative relations are characterized by a quantitative value, e.g.

$$
\mathbf{D} \subseteq \mathbf{O} \times \mathbf{O} \times \mathbf{R}^{+}
$$

with $\mathrm{O}=$ set of objects, $\mathrm{R}^{+}$positive real numbers.

Qualitative relations may ...

- abstract from quantitative values
"contains", "touches"
- express a range of values
d10: $8 \leq d<12$
- express fuzzy relations
"left-of", "above"
- enable soft comparisons fuzzy-set theory


## Qualitative spatial relations

Qualitative spatial relations are expressed by "linguistic variables" (fuzzy variables, symbols with fuzzy values)

Example: "in front of" (ifo)


## Combining Fuzzy Propositions

## Example: Combining fuzzy spatial relations

"Look for a red light in front of a house and above the entrance"
(light1 in-front-of house1, 0.7) and (light1 above entrance1, 0.4)
(light2 in-front-of house2, 0.5) and (light2 above entrance2, 0.6)
Which light matches the description best?

Formal conjunction of fuzzy values:
$[\mathrm{x}, \delta(\mathrm{x})],[\mathrm{y}, \delta(\mathrm{y})], 0 \leq \delta() \leq 1 \quad \delta(\mathrm{x} \& \mathrm{y})=$ ?
alternative 1: $\quad \delta(x \& y)=\delta(x) \cdot \delta(y) \quad$ product of fuzzy values
alternative 2: $\quad \delta(x \& y)=\min \{\delta(x), \delta(y)\} \quad$ minimum of fuzzy values

Probability theory provides a better foundation for uncertainty management


## Recognition of Views by Qualitative 2D-Spatial Relations

Development of "spectacles" for the blind in project MOVIS:

- spectacles contain 2 mini cameras
- blind person may store important views (view models are generated automatically)
- view model can be used to recognize a view during walking

Technical problem:
How can one determine the correspondence of a test view with a model view in spite of

- changed perspective
- changed illumination
- changed objects?



## Relational Description of Views

## Principle:

- description of views by "interesting" image elements and their spatial relations
- use of straight edges and their properties as "interesting" image elements

|  |  | orientientation: | [..] |
| :---: | :---: | :---: | :---: |
| straight edge | properties of an | length: | [..] |
| with left and | edge | I-mean/variance-left: | (, ) |
| right | ( 1 =intensity, | I-mean/variance-right: | (, ) |
| environment | H = hue | H-mean/variance-left: | (, ) |
|  | S = saturation): | H-mean/variance-right: | (, ) |
| $1{ }^{1}$ |  | S-mean/variance-left: | (, ) |
|  |  | S-mean/variance-right: | (, ) |
|  |  | I-contrast: | [-1 .. +1] |
| - |  | H-contrast: | [-1 .. +1] |
|  |  | S-contrast: | [-1 .. +1] |
| -171-1 |  | total contrast: | [-1 .. +1] |
|  |  | significance: | [0.. 1] |

## Location Relation between Edges

Possible relative locations of 2 edges are described by "offset regions"

For test views:

- uncertain reference points

image elements

offset region

For model views:

- uncertain reference points
- uncertain depth values
- uncertain perspective

image elements offset region


## Compatibility Test for Location Relation

Is the spatial relation of a test pair of edges compatible with the spatial relation of a model pair of edges?

model view

test view

offset region for m1 and m2

offset region for t1 and t2

compatibility test by intersecting the offset regions
(empty = incompatible)

## Determining Offset Regions



Determine the image of $P$, if

- the camera is translated by $\Delta t=[\Delta x, \Delta y, \Delta z]$ and rotated by $[\Delta \alpha, \Delta \beta, \Delta \gamma]$,
- the depth of $P$ is given by an uncertainty interval of $\left[z_{p-\min } z_{p-m a x}\right]$

Perspective projection applied to boundary values of uncertainty intervals provides corner points of offset region.

## Offset Regions for Different Uncertainty Intervals

|  |  | $a$ | $b$ | $c$ | $d$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\left[\Delta x_{\min } \Delta x_{\text {max }}\right]$ | $:$ | $[-1 m+1 m]$ | $[-1 m+1 m]$ | $[-1 m+1 m]$ | $[-1 m+1 m]$ |
| $\left[z 1_{\min } z 1_{\text {max }}\right]$ | $:$ | $[19 m 21 m]$ | $[19 m 21 m]$ | $[9 m 51 m]$ | $[9 m 51 m]$ |
| $\left[z 2_{\min } z 2_{\text {max }}\right]$ | $:$ | $[29 m 31 m]$ | $[9 m 51 m]$ | $[29 m 31 m]$ | $[9 m 51 m]$ |
| $\left[\Delta \gamma_{\min } \Delta \gamma_{\text {max }}\right]$ | $:$ | $\left[-5^{\circ}+5^{\circ}\right]$ | $\left[-5^{\circ}+5^{\circ}\right]$ | $\left[-5^{\circ}+5^{\circ}\right]$ | $\left[-5^{\circ}+5^{\circ}\right]$ |




## Basic Idea

- Determine interest points in image
- Determine local image properties around interest points
- Use local image properties for object classification


Example: Interest points determined by Haralick Operator


Example: Gabor-Filterbank for local image description

## Interest Operators (1)

Moravec interest operator: $\mathbf{M}(\mathbf{i}, \mathbf{j})=\frac{1}{8} \sum_{m=i-1}^{i+1} \sum_{n=j-1}^{j+1}|g(m, n)-\mathbf{g}(\mathbf{i}, \mathbf{j})|$


## Zuniga-Haralick operator:

- fit a cubic polynomial

$$
f(i, j)=c_{1}+c_{2} x+c_{3} y+c_{4} x^{2}+c_{5} x y+c_{6} y^{2}+c_{7} x^{3}+c_{8} x^{2} y+c_{9} x y^{2}+c_{10} y^{3}
$$

For a $5 \times 5$ neighbourhood the coefficients of the best-fitting polynomial can be directly determined from the $\mathbf{2 5}$ greyvalues

- compute interest value from polynomial coefficients

$$
Z H(i, j)=\frac{-2\left(c_{2}^{2} c_{6}-c_{2} c_{3} c_{5}-c_{3}^{2} c_{4}\right)}{\left(c_{2}^{2}+c_{3}^{2}\right)^{\frac{3}{2}}} \quad \text { measure of "cornerness" of the polynomial }
$$

## Interest Operators (2)

## Difference-of-Gaussians (DoG)

Locates edges at zero crossings of second derivative of smoothed image


Harris interest operator:
Determine points with two strong principle curvatures

$$
R=\operatorname{det}(H)-k \operatorname{tr}(H)=\alpha \beta-k(\alpha+\beta)
$$

$\alpha$ and $\beta$ are eigenvalues of Hessian matrix $H$ and proportional to main curvatures

$$
\mathrm{H}=\left[\begin{array}{ll}
D_{x x} & D_{x y} \\
D_{x y} & D_{y y}
\end{array}\right]
$$

## SIFT Features

SIFT = Scale Invariant Image Features

David G. Lowe: Distinctive Image Features from Scale-Invariant Keypoints International Journal of Computer Vision, 2004

## Computation Steps for SIFT Features

1. Scale-space extrema detection: The first stage of computation searches over all scales and image locations. It is implemented efficiently by using a difference-of-Gaussian function to identify potential interest points that are invariant to scale and orientation.
2. Keypoint localization: At each candidate location, a detailed model is fit to determine location and scale. Keypoints are selected based on measures of their stability.
3. Orientation assignment: One or more orientations are assigned to each keypoint location based on local image gradient directions. All future operations are performed on image data that has been transformed relative to the assigned orientation, scale, and location for each feature, thereby providing invariance to these transformations.
4. Keypoint descriptor: The local image gradients are measured at the selected scale in the region around each keypoint. These are transformed into a representation that allows for significant levels of local shape distortion and change in illumination.


Figure 1: For each octave of scale space, the initial image is repeatedly convolved with Gaussians to produce the set of scale space images shown on the left. Adjacent Gaussian images are subtracted to produce the difference-of-Gaussian images on the right. After each octave, the Gaussian image is down-sampled by a factor of 2 , and the process repeated.


Figure 2: Maxima and minima of the difference-of-Gaussian images are detected by comparing a pixel (marked with X ) to its 26 neighbors in $3 \times 3$ regions at the current and adjacent scales (marked with circles).

## Keypoint Selection



## Eliminating Edge Responses

Compute Hessian at keypoint:

$$
\mathbf{H}=\left[\begin{array}{ll}
D_{x x} & D_{x y} \\
D_{x y} & D_{y y}
\end{array}\right]
$$

Eigenvalues $\alpha$ and $\beta$ are proportional to principal curvatures.
Both principle curvatures must be significant for a keypoint to be stable.
Note that

$$
\begin{gathered}
\operatorname{Tr}(\mathbf{H})=D_{x z}+D_{y y}=\alpha+\beta \\
\operatorname{Det}(\mathbf{H})=D_{x x} D_{y y}-\left(D_{x y}\right)^{2}=\alpha \beta .
\end{gathered}
$$

Hence one can check the ratio $\mathrm{r}=\alpha / \beta$ of the principle curvatures by evaluating

$$
\frac{\operatorname{Tr}(\mathbf{H})^{2}}{\operatorname{Det}(\mathbf{H})}<\frac{(r+1)^{2}}{r}
$$

## Local Image Descriptor



Figure 7: A keypoint descriptor is created by first computing the gradient magnitude and orientation at each image sample point in a region around the keypoint location, as shown on the left. These are weighted by a Gaussian window, indicated by the overlaid circle. These samples are then accumulated into orientation histograms summarizing the contents over 4 x 4 subregions, as shown on the right, with the length of each arrow corresponding to the sum of the gradient magnitudes near that direction within the region. This fi gure shows a 2 x 2 descriptor array computed from an 8 x 8 set of samples, whereas the experiments in this paper use $4 \times 4$ descriptors computed from a 16 x 16 sample array.

## SIFT Feature Matching

- Find nearest neighbor in a database of SIFT features from training images.
- For robustness, use ratio of nearest neighbor to ratio of second nearest neighbor.
- Neighbor with minimum Euclidean distance => expensive search.
- Use an approximate, fast method to find nearest neighbor with high probability


## Recognition Using SIFT Features

- Compute SIFT features on the input image
- Match these features to the SIFT feature database
- Each keypoint specifies 4 parameters: 2D location, scale, and orientation.
- To increase recognition robustness: Hough transform to identify clusters of matches that vote for the same object pose.
- Each keypoint votes for the set of object poses that are consistent with the keypoint's location, scale, and orientation.
- Locations in the Hough accumulator that accumulate at least 3 votes are selected as candidate object/pose matches.
- A verfication step matches the training image for the hypothesized object/pose to the image using a least-squares fit to the hypothesized location, scale, and orientation of the object.


## Experiments (1)



Figure 12: The training images for two objects are shown on the left. These can be recognized in a cluttered image with extensive occlusion, shown in the middle. The results of recognition are shown on the right. A parallelogram is drawn around each recognized object showing the boundaries of the original training image under the affi ne transformation solved for during recognition. Smaller squares indicate the keypoints that were used for recognition.

## Experiments (2)



Figure 13: This example shows location recognition within a complex scene. The training images for locations are shown at the upper left and the 640x 315 pixel test image taken from a different viewpoint locations are shown at the upper left and the 640x 315 pixel test image taken from a different viewpoint is on the upper night. The recognized regions are shown on the lower image, wim keypoints show transform used for recognition.

## SIFT Features Summary

- SIFT features are reasonably invariant to rotation, scaling, and illumination changes.
- They can be used for matching and object recognition (among other things).
- Robust to occlusion: as long as we can see at least 3 features from the object we can compute the location and pose.
- Efficient on-line matching: recognition can be performed in close-toreal time (at least for small object databases).


## Patch-based Object Categorization and Segmentation

Bastian Leibe, Ales Leonardis, and Bernt Schiele:
Combined Object Categorization and Segmentation with an Implicit Shape Model
In ECCV'04 Workshop on Statistical Learning in Computer Vision, Prague, May 2004.

## Implicit Shape Model - Representation



105 training images
(+ motion segmentation)

- Learn appearance codebook

Extract patches at DoG interest points
Agglomerative clustering $\Rightarrow$ codebook

- Learn spatial distributions

Match codebook to training images
Record matching positions on object


## Implicit Shape Model - Recognition (1)



## Image Patch



## Implicit Shape Model - Recognition (2)



## Car Detection

- Recognizes different kinds of cars
- Robust to clutter, occlusion, noise, low contrast



## Cow Detection

- frame-by-frame detection
- no temporal continuity exploited


