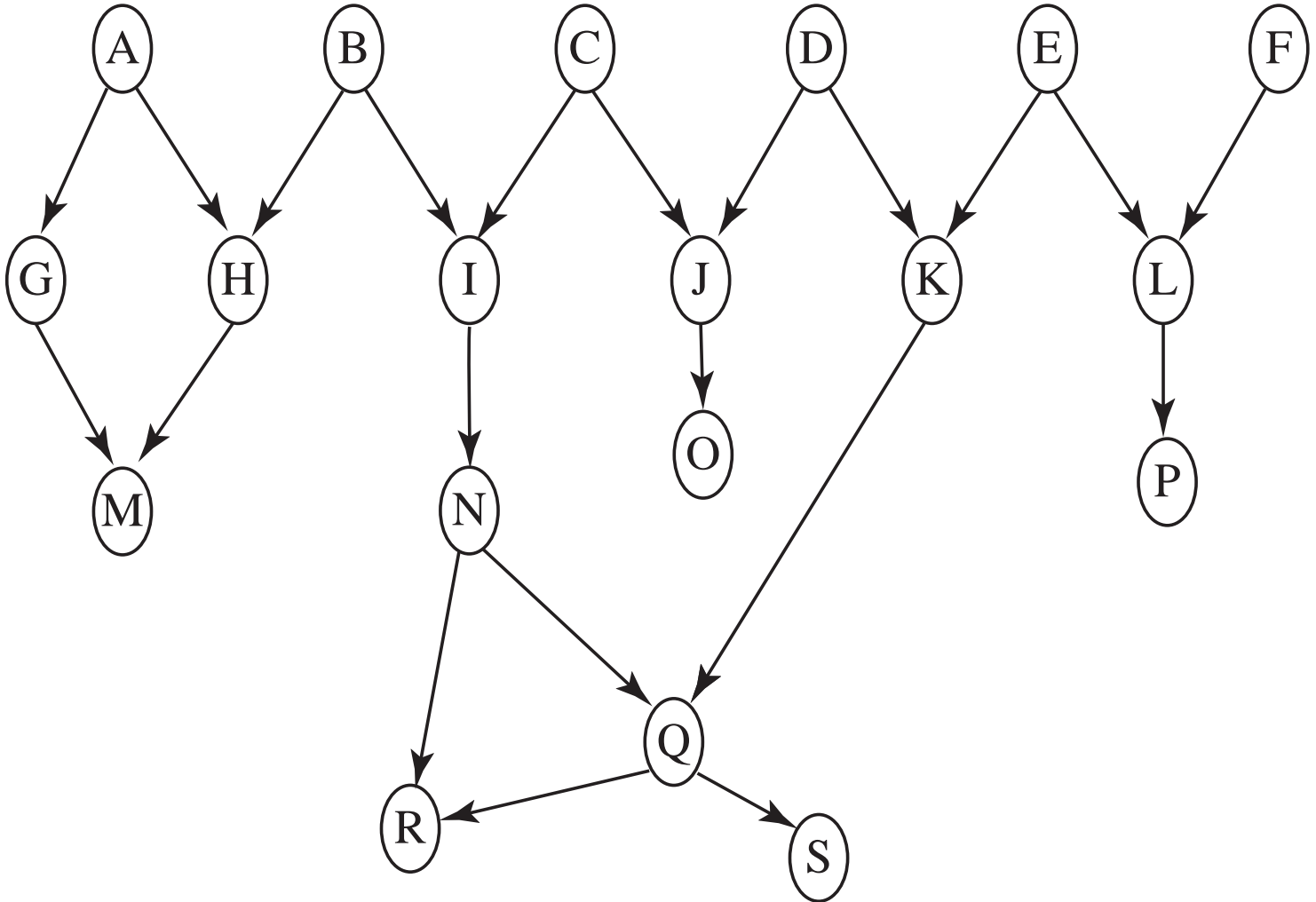


Understanding independence: example



Understanding independence: questions

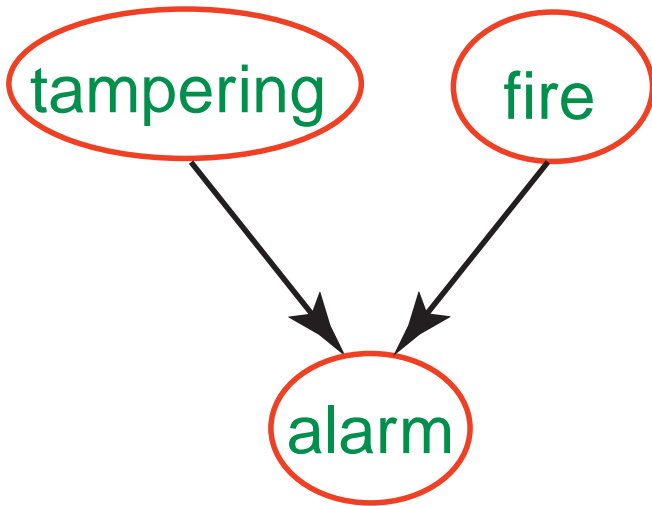
- On which given probabilities does $P(N)$ depend?
- If you were to observe a value for B , which variables' probabilities will change?
- If you were to observe a value for N , which variables' probabilities will change?
- Suppose you had observed a value for M ; if you were to then observe a value for N , which variables' probabilities will change?
- Suppose you had observed B and Q ; which variables' probabilities will change when you observe N ?



What variables are affected by observing?

- If you observe variable \bar{Y} , the variables whose posterior probability is different from their prior are:
 - The ancestors of \bar{Y} and
 - their descendants.
- Intuitively (if you have a causal belief network):
 - You do **abduction** to possible causes and
 - **prediction** from the causes.

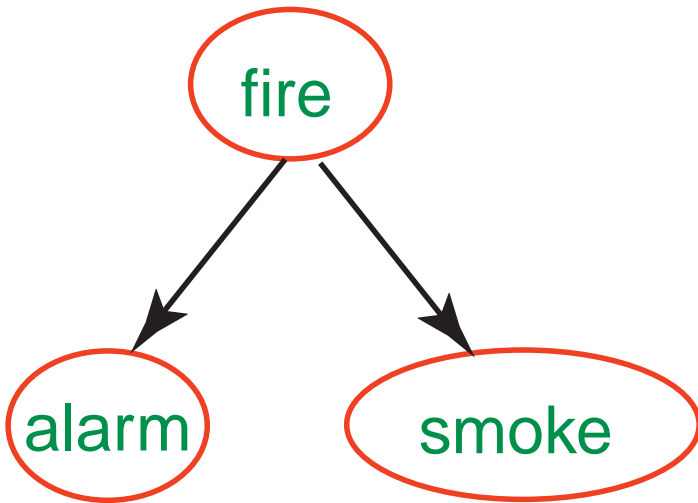
Common descendants



- *tampering* and *fire* are independent
- *tampering* and *fire* are dependent given *alarm*
- Intuitively, *tampering* can **explain away** *fire*

Common ancestors

- *alarm* and *smoke* are dependent
- *alarm* and *smoke* are independent given *fire*
- Intuitively, *fire* can **explain** *fire* and *smoke*; learning one can affect the other by changing your belief in *fire*.

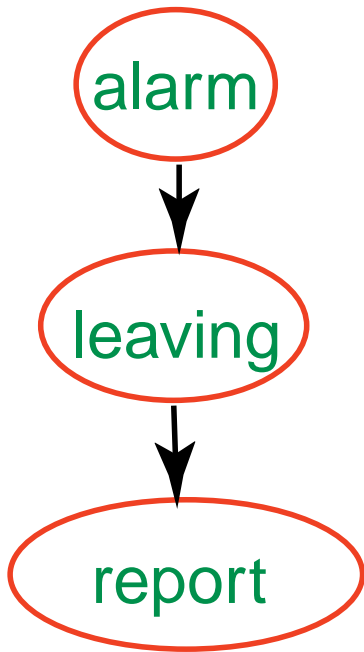


Chain

➤ *alarm* and *report* are dependent

➤ *alarm* and *report* are independent given *leaving*

➤ Intuitively, the only way that the *alarm* affects *report* is by affecting *leaving*.



d-separation

- ▶ \bar{X} is **d-separated** from \bar{Y} given \bar{Z} if there is no path from an element of \bar{X} to an element of \bar{Y} , where:
 - ▶ If there are paths $A \rightarrow B$ and $B \rightarrow C$ such that $B \notin \bar{Z}$, there is a path $A \rightarrow C$.
 - ▶ If there are paths $B \rightarrow A$ and $B \rightarrow C$ such that $B \notin \bar{Z}$, there is a path $A \rightarrow C$.
 - ▶ If there are paths $A \rightarrow B$ and $C \rightarrow B$ such that $B \in \bar{Z}$, there is a path $A \rightarrow C$.
- ▶ \bar{X} is independent \bar{Y} given \bar{Z} for some conditional probabilities iff \bar{X} is d-separated from \bar{Y} given \bar{Z}

