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 $r = \sum_{mn} g_{mn} t_{mn}$  cross-correlation between image  $g_{mn}$  and template  $t_{mn}$ Compare with squared Euclidean distance  $d_e^2$ :

$$d_e^2 = \sum_{mn} (g_{mn} - t_{mn})^2 = \sum_{mn} g_{mn}^2 + \sum_{mn} t_{mn}^2 - 2r$$

Image "energy"  $\Sigma g_{mn}{}^2$  and template "energy"  $\Sigma t_{mn}{}^2$  correspond to length of feature vectors.

$$r^{\,\prime}=\frac{\displaystyle\sum_{mn}g_{mn}t_{mn}}{\displaystyle\sqrt{\displaystyle\sum_{mn}g_{mn}^{2}\sum_{mn}t_{mn}^{2}}}$$

Normalized cross-correlation is independent of image and template energy. It measures the cosine of the angle between the feature vectors in MN-space.

**Cauchy-Schwartz Inequality:** 

 $|\mathbf{r}'| \le 1$  with equality iff  $g_{mn} = c t_{mn}$ , all mn

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