









































$$\begin{split} r &= \sum_{mn} g_{mn} t_{mn} & \text{cross-correlation between image } g_{mn} \text{ and template } t_{mn} \\ \text{Compare with squared Euclidean distance } d_e^2: \\ d_e^2 &= \sum_{mn} (g_{mn} - t_{mn})^2 = \sum_{mn} g_{mn}^2 + \sum_{mn} t_{mn}^2 - 2r \\ \text{Image "energy" } \Sigma g_{mn}^2 \text{ and template "energy" } \Sigma t_{mn}^2 \text{ correspond to length of feature vectors.} \\ r' &= \frac{\sum_{mn} g_{mn} t_{mn}}{\sqrt{\sum_{mn} g_{mn}^2 \sum_{mn} t_{mn}^2}} & \text{Normalized cross-correlation is independent of image and template energy. It measures the cosine of the angle between the feature vectors in MN-space.} \end{split}$$

Cauchy-Schwartz Inequality:

 $|\mathbf{r}'| \le 1$ with equality iff $g_{mn} = c t_{mn}$, all mn

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