# **Motion Analysis**

Motion analysis of digital images is based on a temporal sequence of image frames of a coherent scene.

"sparse sequence"	=> few frames, temporally spaced apart, considerable differences between frames
"dense sequence"	=> many frames, incremental time steps, incremental differences between frames
video	=> 50 half frames per sec, interleaving, line-by-line sampling

#### Motion detection

Register locations in an image sequence which have change due to motion

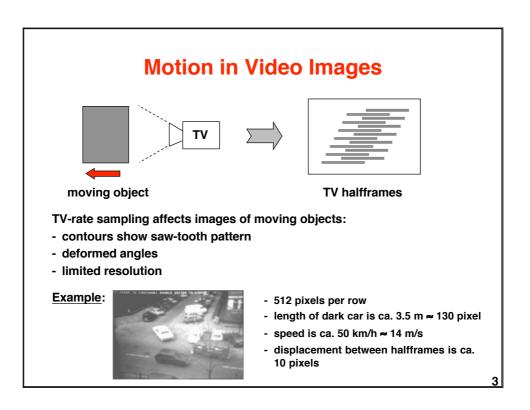
## Moving object detection and tracking

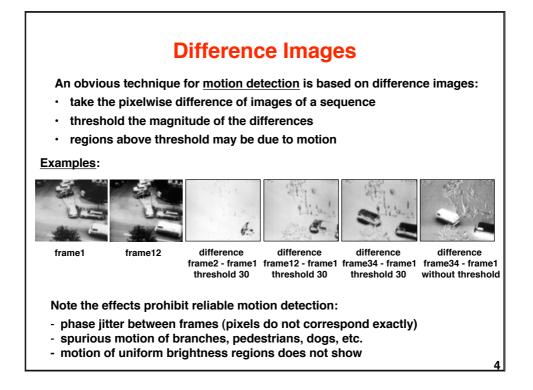
Detect individual moving objects, determine and predict object trajectories, track objects with a moving camera

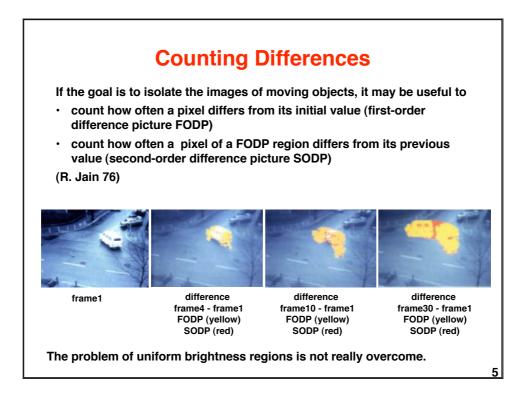
### **Derivation of 3D object properties**

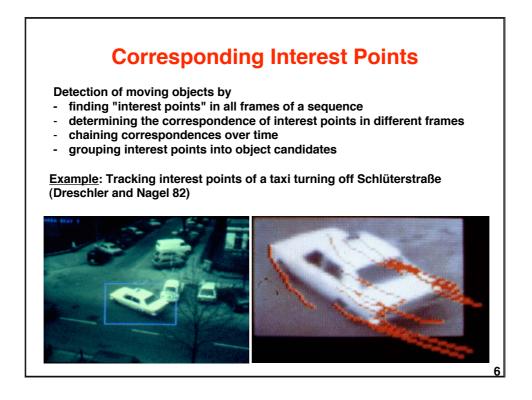
Determine 3D object shape from multiple views ("shape from motion")

**Case Distinctions for Motion Analysis** B/W images stationary observer polyeder moving observer colour images smooth objects arbitrary objects single moving object xray images matte surfaces multiple moving objects **IR** images natural images specular surfaces rigid objects textured surfaces jointed objects noisy data arbitrary surfaces deformable objects ideal data without occlusion perspective projection monocular images with occlusion weakly perspective projection stereo images orthographic projection uncalibrated camera dense flow calibrated camera rotation only sparse flow translation only no flow data-driven unrestricted motion paralaxis expectation-driven quatitative motion 2 image analysis real-time multiple image analysis qualitative motion no real-time incremental motion small objects parallel computation extended objects large-scale motion sequential computation Many motion analysis methods are only applicable in restricted cases!











Interest points (feature points) are image locations where an interest operator computes a high value. Interest operators measure properties of a local pixel neighbourhood.

Moravec interest operator:  $M(i, j) = \frac{1}{8} \sum_{m=i-1}^{i+1} \sum_{m=i-1}^{j+1} |g(m,n) - g(i, j)|$ 

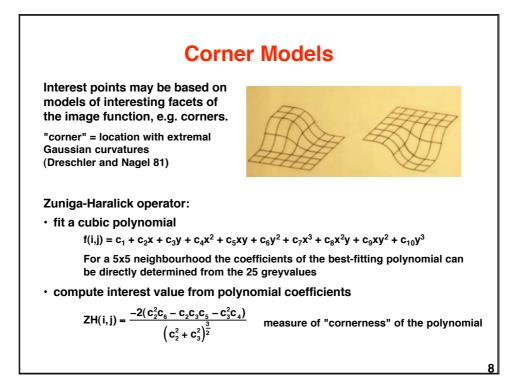


This simple operator measures the distinctness of a point w.r.t. its surround.

Refinement of Moravec operator: Determine locations with strong brightness variations along two orthogonal directions (e.g. based on variances in horizontal, vertical and diagonal direction).



Interest points in different frames may not correspond to identical physical object parts due to their small neighbourhood and noise.



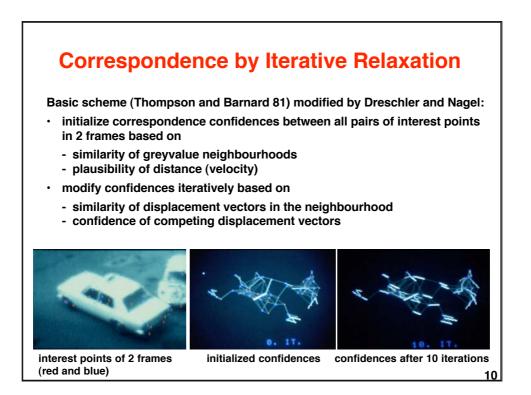


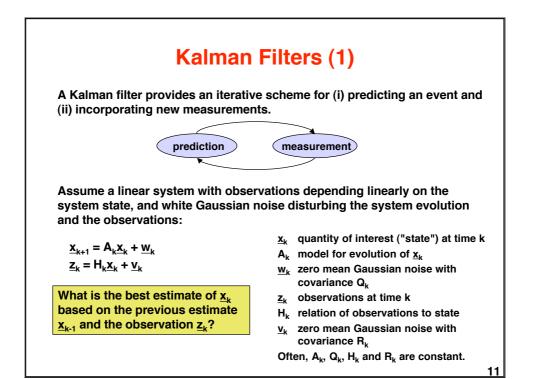
The correspondence problem is to determine which interest points in different frames of a sequence mark the same physical part of a scene.

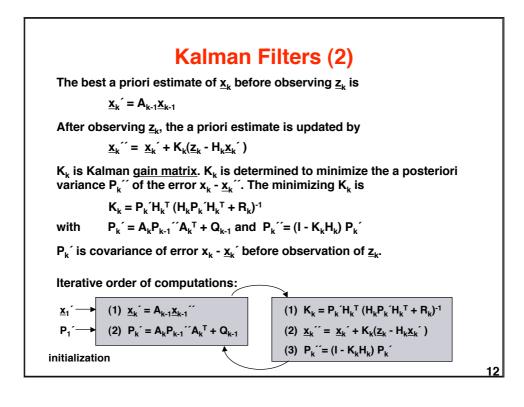
**Difficulties:** 

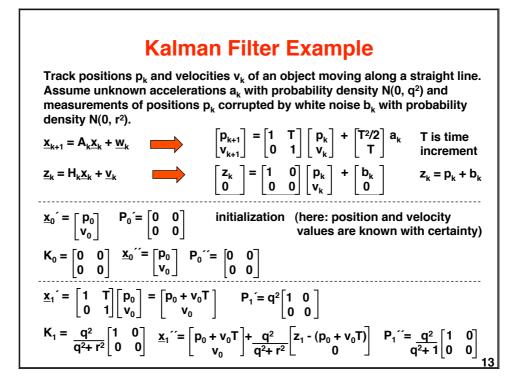
- · scene may not offer enough structure to uniquely locate points
- · scene may offer too much structure to uniquely locate points
- · geometric features may differ strongly between frames
- photometric features differ strongly between frames
- there may be no corresponding point because of occlusion

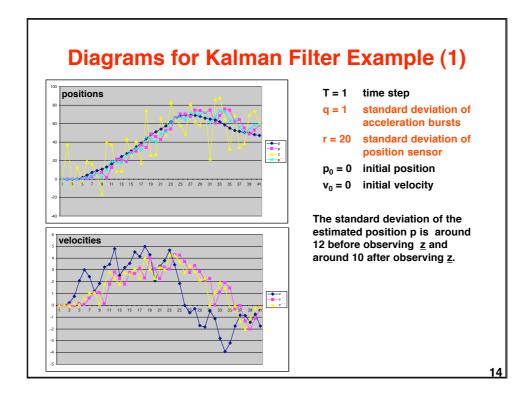
Note that these difficulties apply to single-camera motion analysis as well as multiple-camera 3D analysis (e.g. binocular stereo).

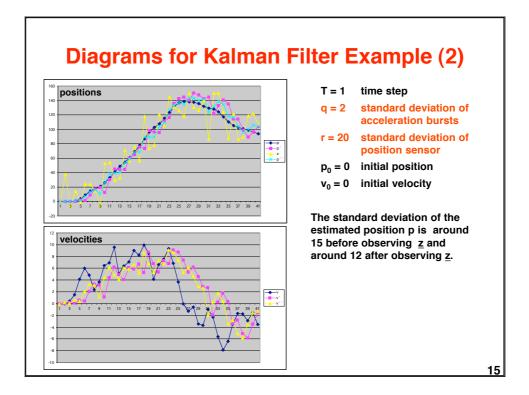


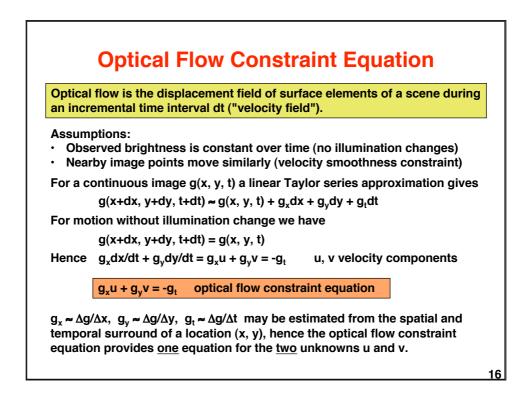


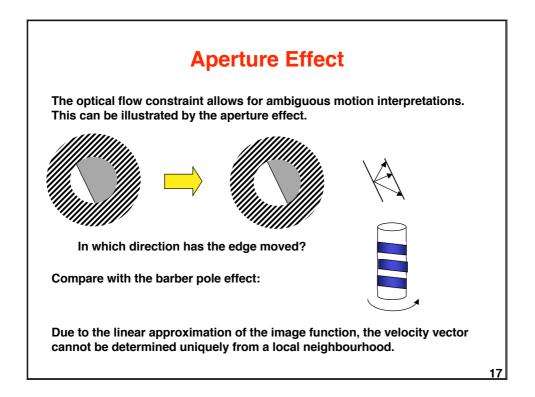


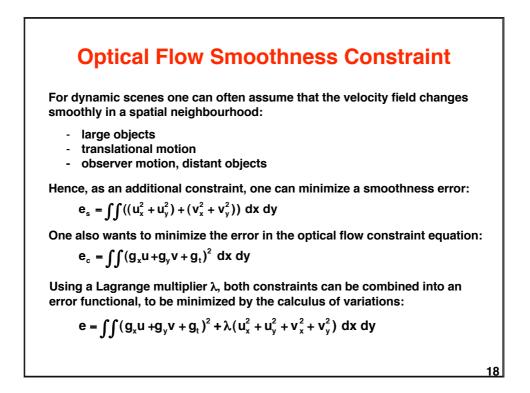


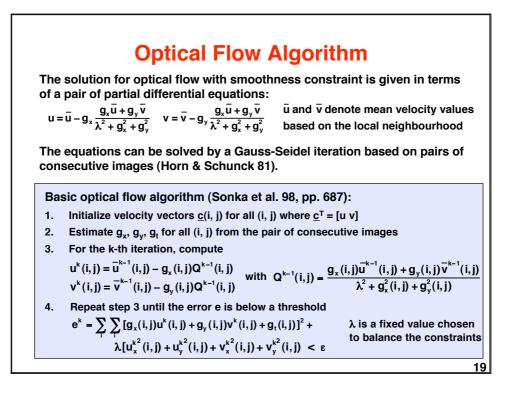


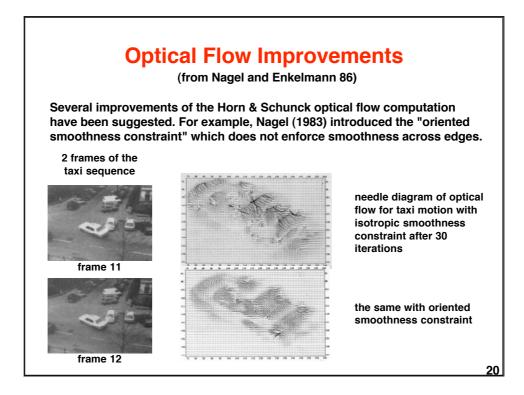


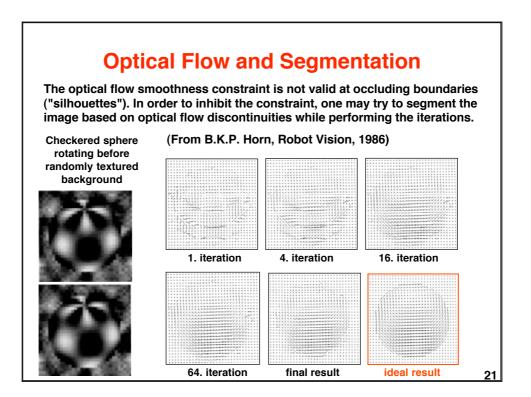


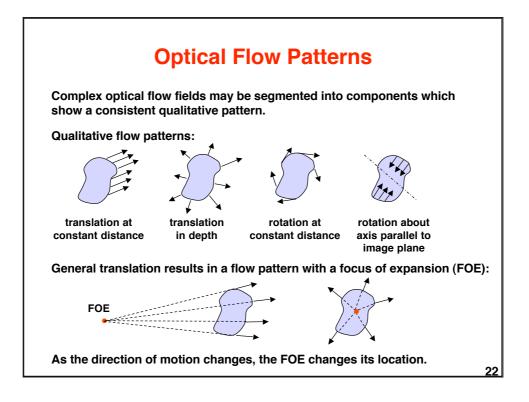


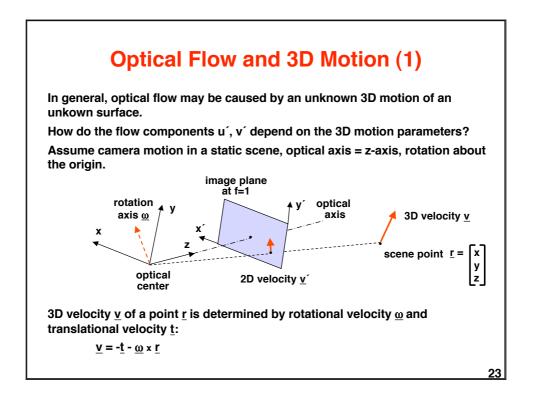












## **Optical Flow and 3D Motion (2)**

By taking the component form of  $\underline{v} = -\underline{t} - \underline{\omega} \times \underline{r}$  with  $\underline{t}^T = [t_x, t_y, t_z], \underline{\omega}^T = [a, b, c]$ and  $\underline{r}^T = [x \ y \ z]$  and computing the perspective projection we get

$$\mathbf{u}' = \frac{\mathbf{x}}{\mathbf{z}} - \frac{\mathbf{x}\mathbf{z}}{\mathbf{z}^2} = \left(-\frac{\mathbf{t}_x}{\mathbf{z}} - \mathbf{b} + \mathbf{c}\mathbf{y}'\right) - \mathbf{x}'\left(-\frac{\mathbf{t}_z}{\mathbf{z}} - \mathbf{a}\mathbf{y}' + \mathbf{b}\mathbf{x}'\right)$$
$$\mathbf{v}' = \frac{\dot{\mathbf{y}}}{\mathbf{z}} - \frac{\mathbf{y}\dot{\mathbf{z}}}{\mathbf{z}^2} = \left(-\frac{\mathbf{t}_y}{\mathbf{z}} - \mathbf{c}\mathbf{x}' + \mathbf{a}\right) - \mathbf{y}'\left(-\frac{\mathbf{t}_z}{\mathbf{z}} - \mathbf{a}\mathbf{y}' + \mathbf{b}\mathbf{x}'\right)$$

Observation of u and v at location (x', y') gives 2 equations for 7 unknowns. Note that motion of a point at distance kz with translation kt and the same rotation  $\omega$  will give the same optical flow, k any scale factor.

The translational and rotational parts may be separated:

$$u'_{\text{translation}} = -\frac{t_x + x't_z}{z} \qquad u'_{\text{rotation}} = ax'y' - b(x'^2 + 1) + cy'$$
$$v'_{\text{translation}} = -\frac{t_y + y't_z}{z} \qquad v'_{\text{rotation}} = a(y'^2 + 1) - bx'y' + cx'$$

For pure translation we have 2 equations for 3 unknows (z fixed arbitrarily).

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