



Universität Hamburg

DER FORSCHUNG | DER LEHRE | DER BILDUNG

**MIN-Fakultät**  
**Fachbereich Informatik**  
Arbeitsbereich SAV/BV (KOGS)

# Image Processing 1 (IP1)

## Bildverarbeitung 1

Lecture 22: Object Recognition 2

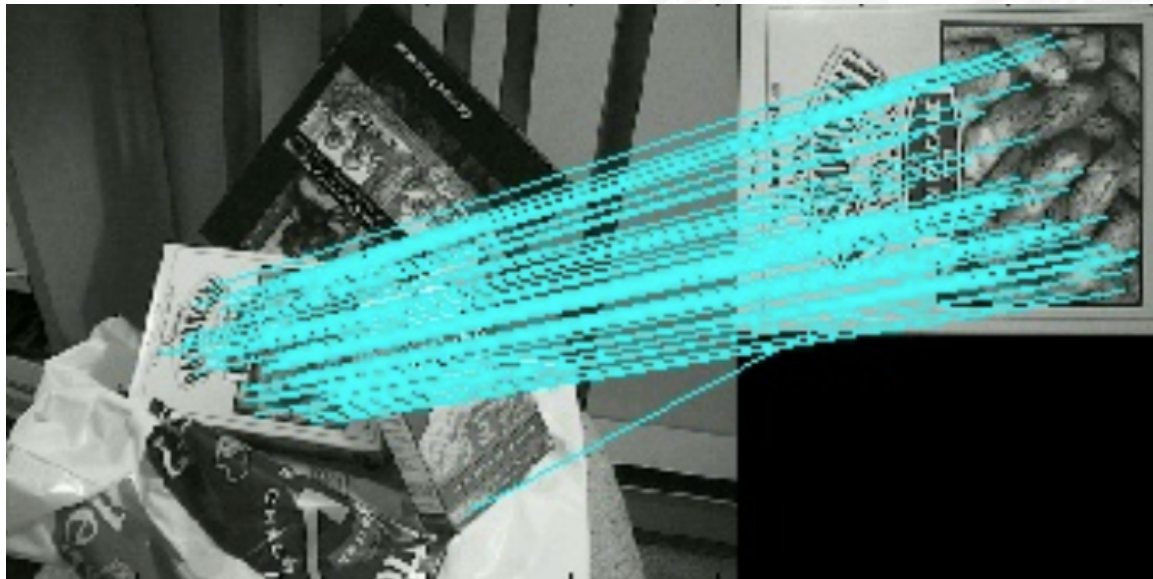
Winter Semester 2014/15

Dr. Benjamin Seppke  
Prof. Siegfried Stiehl

# Object Recognition with Local Descriptors

Basic idea:

- Determine interest points in model images
- Determine invariant local image properties around interest points
- Use local image properties for finding matching objects



Matching images using SIFT features  
(SIFT = Scale-Invariant Feature Transform)

# SIFT Method

David G. Lowe: Distinctive Image Features from Scale-Invariant Keypoints  
International Journal of Computer Vision, 2004 (Protected by US patent)

Lowe developed specific methods for:

1. Determining invariant local descriptors at interest points
  - finding stable interest points ("keypoints")
  - computing largely scale-invariant features at interest points
2. Extracting stable descriptors for object models
3. Finding and recognizing objects based on local descriptors

# Determining SIFT Keypoints: Scale Space

**Keypoints are local maxima and minima in the DoG of scaled images.**

Recall:

$$L(x, y, k\sigma) = G(x, y, k\sigma) * I(x, y)$$

Convolution of image  $I(x, y)$  with Gaussian  $G(x, y, k\sigma)$

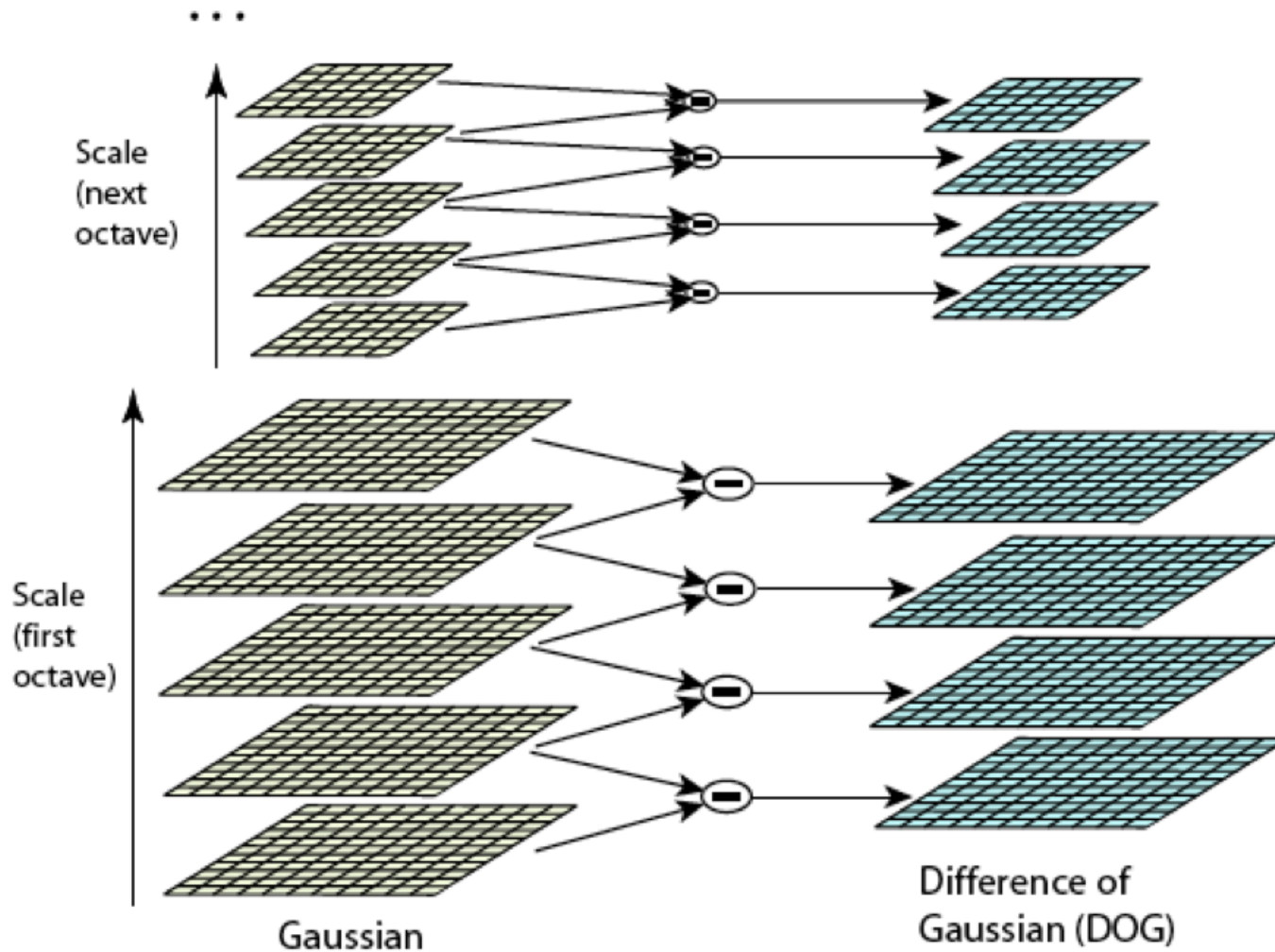
$$D(x, y, \sigma) = L(x, y, k_i\sigma) - L(x, y, k_j\sigma)$$

Difference of Gaussians (DoG)

Procedure:

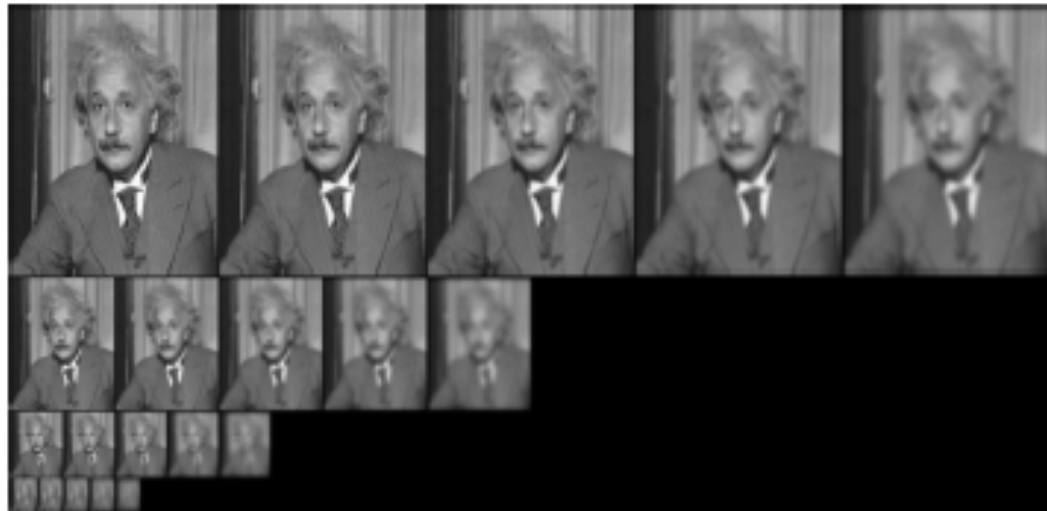
- a) Initial image is repeatedly convolved with Gaussians of multiples of  $\sigma$ , forming a scale space.
- b) Scaled images within an octave ( $\sigma \dots 2\sigma$ ) have same resolution. Adjacent scales are subtracted to produce DoGs.
- c) Scaled images are down-sampled from one octave to the next.

# Illustration of SIFT Scale Space



# Example Image in SIFT Scale Space

5 Gaussian filtered images per octave

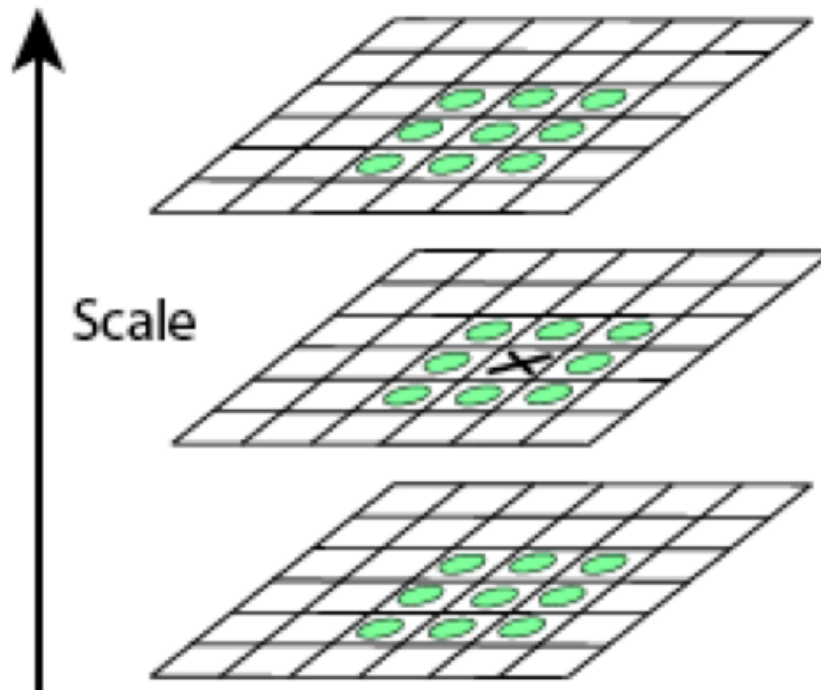


Corresponding DoGs



# Determining Extrema

Find local minima and maxima by comparing a DoG pixel to its 26 neighbours in 3x3 regions at the current and adjacent scales.



# Sub-pixel Localization of Extrema

- Take extrema of previous step as keypoint candidates
- Determine Taylor expansion at candidate location
- Find subpixel extremum by setting derivatives to zero
- If location of subpixel extremum is within 0.5 of candidate location (in x- or y-direction), keep keypoint at subpixel location, otherwise discard keypoint candidate
- If value of expansion at subpixel location is less than 0.03, discard keypoint

Taylor expansion:

$$D(x, y) = D + x \frac{\partial D}{\partial x} + y \frac{\partial D}{\partial y} + \frac{1}{2} x^2 \frac{\partial^2 D}{\partial x^2} + \frac{1}{2} y^2 \frac{\partial^2 D}{\partial y^2} + xy \frac{\partial^2 D}{\partial x \partial y}$$

approximated from  
local neighbourhood

Extrema:

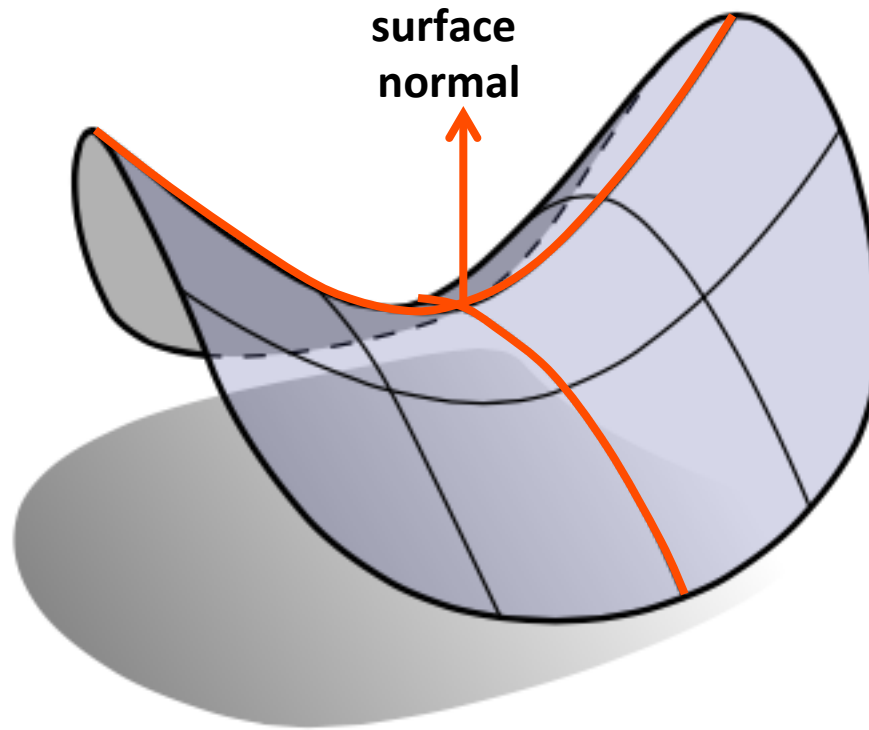
$$x_{ext} = \frac{D_y D_{xy} - D_x D_{yy}}{D_{xx} D_{yy} - D_{xy}^2} \quad y_{ext} = \frac{D_x D_{xy} - D_y D_{xx}}{D_{xx} D_{yy} - D_{xy}^2} \quad \text{with} \quad D_x = \frac{\partial D}{\partial x} \text{ etc.}$$



# Eliminating Edge Responses

- Keypoints at strong edges tend to be unstable. Principal curvatures at keypoint must be significant for keypoint to be stable.
- Compute Hessian at keypoint:  $H = \begin{pmatrix} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{pmatrix}$
- Eigenvalues  $\alpha$  and  $\beta$  of H are proportional to principal curvatures.
- Note that  $R = \frac{Tr(H)^2}{Det(H)} = \frac{(r+1)^2}{r}$  with  $r = \frac{\alpha}{\beta}$ ,  $tr(H) = D_{xx} + D_{yy} = \alpha + \beta$   
 $det(H) = D_{xx}D_{yy} - (D_{xy})^2 = \alpha\beta$
- The higher the absolute differences of principal curvatures of D, the higher the value of R.
- Hence if  $R > \frac{(r_0 + 1)^2}{r_0}$  with  $r_0$  as threshold, the keypoint is discarded.

# Illustration of Principal Curvatures



Each point of a 3D surface has a maximum and minimum curvature.

# Assigning Orientations

Each keypoint is marked by one or more dominant orientations based on image gradient directions computed in a neighbouring region.

Gradient magnitude:

$$m(x, y) = \sqrt{(L(x+1, y) - L(x-1, y))^2 + (L(x, y+1) - L(x, y-1))^2}$$

Gradient direction:

$$\theta(x, y) = \text{atan2}[L(x, y+1) - L(x, y-1), L(x+1, y) - L(x-1, y)]$$

Gradient magnitudes, weighted by a Gaussian of radius  $1.5\sigma$ , are summed in 36 bins of an orientation histogram. The histogram peak and all other peaks within 80% of the absolute peak value are assigned as dominant keypoint orientations.

**Dominant keypoint orientations are used to achieve orientation invariance for object recognition.**

# Illustration of Keypoint Selection I



**233 x 189 greyvalue image**



**832 keypoint candidates at extrema of DoG images. Vectors show location, orientation and scale.**

# Illustration of Keypoint Selection II



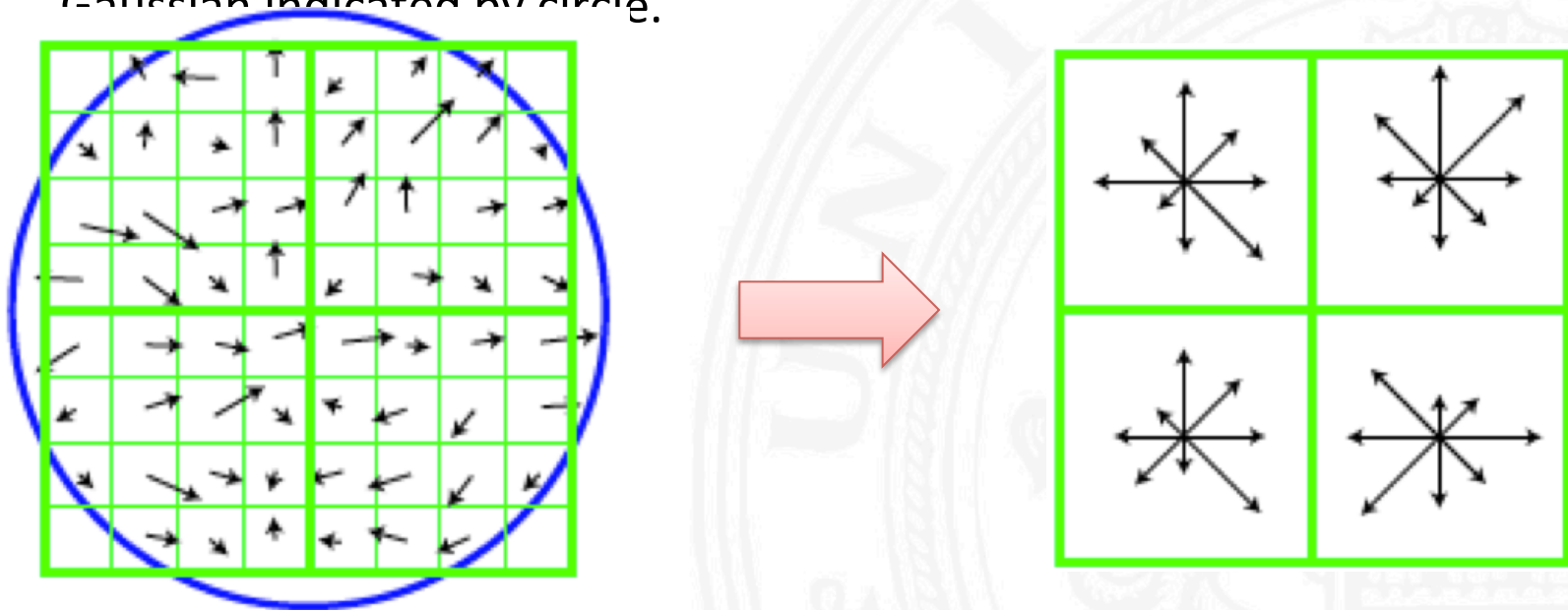
**729 keypoints remain after applying threshold on minimum contrast**



**536 keypoints remain after applying threshold on ratio of principal curvatures**

# Computing a Keypoint Descriptor

- 4 x 4 orientation histograms with 8 bins each are determined from a 16 x 16 neighbourhood of a keypoint. Each bin contains the sum of the gradient magnitudes of corresponding orientations, weighted by a Gaussian.
- Illustration shows 2 x 2 histograms for 8 x 8 neighbourhood, Gaussian indicated by circle.



# Recognition Using SIFT Features

- Compute SIFT features on the input image
- Match these features to the SIFT feature database of an object model
- Each keypoint specifies 4 parameters: 2D location, scale, and dominant orientation.
- To increase recognition robustness: Hough transform to identify clusters of matches that vote for the same object pose.
- Each keypoint votes for the set of object poses that are consistent with the keypoint's location, scale, and orientation.
- Locations in the Hough accumulator that accumulate at least 3 votes are selected as candidate object/pose matches.
- A verification step matches the training image for the hypothesized object/pose to the image using a least-squares fit to the hypothesized location, scale, and orientation of the object.

# Experiment 1 I



Training images



Test image



# Experiment 1 II

Test image with overlaid results.

Parallelograms show locations of recognized objects.

Small squares show keypoints used for recognition.



# Experiment 2 I



Complex test image, 640 x 315 pixels

# Experiment 2 II



Training images taken from independent viewpoints

# Experiment 2 III



## Results

# SIFT Features Summary

- SIFT features are reasonably invariant to rotation, scaling, and illumination changes.
- They can be used for matching and object recognition (among other things).
- Robust to occlusion: as long as we can see at least 3 features from the object we can compute the location and pose.
- Efficient on-line matching: recognition can be performed in close-to-real time (at least for small object databases).

# Combined Object Categorization and Segmentation

Bastian Leibe, Ales Leonardis, and Bernt Schiele: Combined Object Categorization and Segmentation with an Implicit Shape Model

ECCV'04 Workshop on Statistical Learning in Computer Vision, Prague, May 2004.

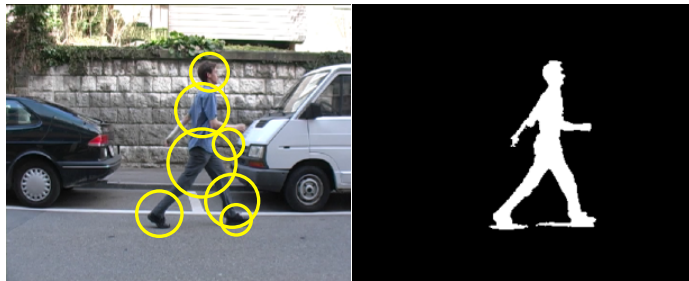
Define a shape model for an object class (or category) by

- a class-specific collection of local appearances (a "codebook"),
- a spatial probability distribution specifying where a codebook entry may be found on the object

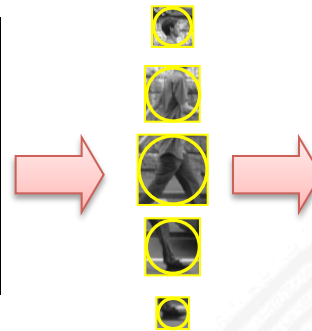
To recognize an object,

- extract image patches around interest points and compare them with the codebook.
- Matching patches cast probabilistic votes leading to object hypotheses.
- Each pixel of an object hypothesis is classified as object or background based on the contributing patches.

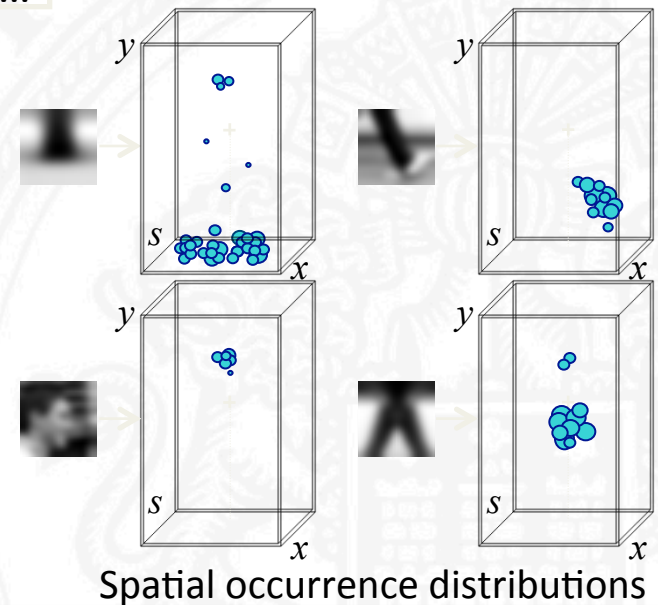
# Implicit Shape Model - Representation



105 training images  
(+ motion segmentation)



- Learn appearance codebook
  - Extract 25x25 patches at interest points
  - Agglomerative clustering  $\Rightarrow$  codebook
- Learn spatial distributions
  - Match codebook to training images
  - Record matching positions on object



# Harris Corner Detector I

Large differences between a pixel and its surroundings:

$$S(x, y) = \sum_u \sum_v w(u, v) (I(u+x, v+y) - I(u, v))^2$$

Averaging over a circular window with Gaussian weights  $w(u, v)$ .

First-order Taylor Series approximation:

$$I(u+x, v+y) \approx I(u, v) + I_x(u, v)x + I_y(u, v)y$$

$$\Rightarrow S(x, y) \approx \sum_u \sum_v w(u, v) (I_x(u, v)x + I_y(u, v)y)^2 = [x \quad y] A \begin{bmatrix} x \\ y \end{bmatrix}$$

with  $A = \sum_u \sum_v w(u, v) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$  "Structure Tensor"



# Harris Corner Detector II

- Eigenvalues  $\lambda_1$  and  $\lambda_2$  of  $A$  indicate cornerness:
  - $\lambda_1 \approx 0$  and  $\lambda_2 \approx 0$  basically flat greyvalues
  - $\lambda_1 \approx 0$  and  $\lambda_2 \gg 0$  edge
  - $\lambda_1 \gg 0$  and  $\lambda_2 \gg 0$  corner
- Instead of computing eigenvalues explicitly:
  - $M_c = \lambda_1 \lambda_2 - \kappa(\lambda_1 + \lambda_2)^2 = \mathbf{det}(A) - \kappa \mathbf{trace}^2(A)$   
measure of cornerness
  - $\kappa = 0.04 \dots 0.15$  sensitivity parameter, must be tuned empirically

# Agglomerative Clustering

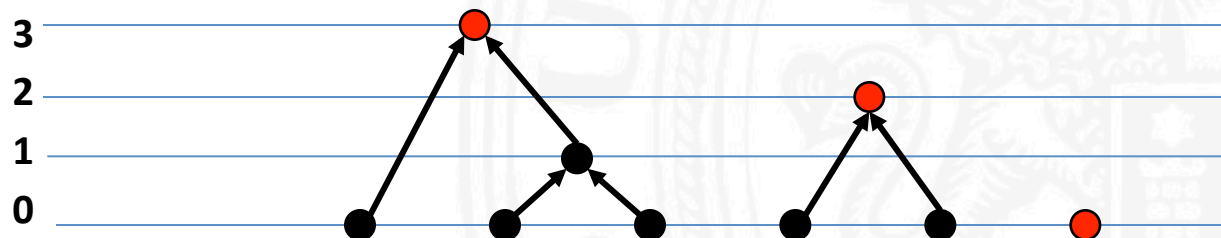
- Start with separate clusters for each single item
- Merge most similar clusters as long as average similarity within cluster stays above threshold

$$s(C) = \frac{\sum_{p \in C} NGC(p)}{|C|}$$

similarity  $s$  within cluster  $C$

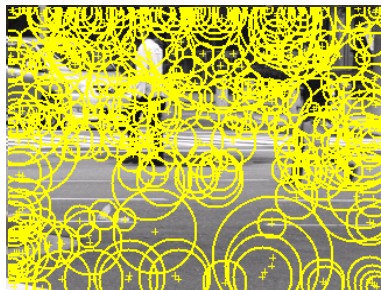
$$NGC(p, q) = \frac{\sum_i (p_i - \bar{p})(q_i - \bar{q})}{\sqrt{\sum_i (p_i - \bar{p})^2 \sum_i (q_i - \bar{q})^2}}$$

Normalized Greyscale Correlation



# Implicit Shape Model - Recognition I

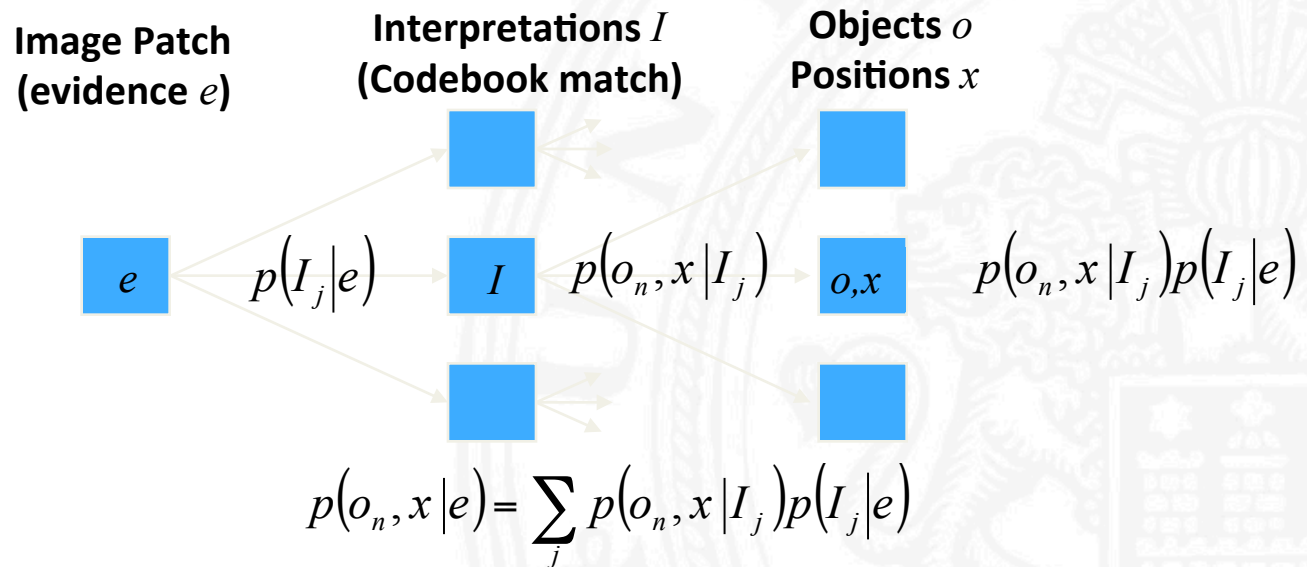
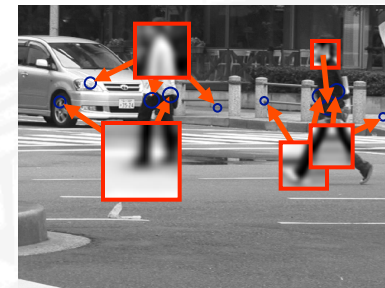
Interest Points



Matched Codebook Entries



Probabilistic Voting



# Implicit Shape Model - Recognition II

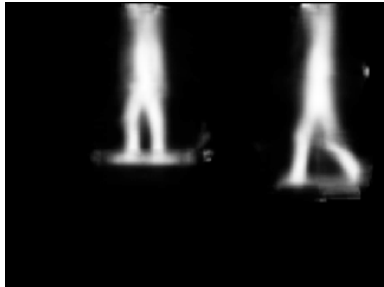
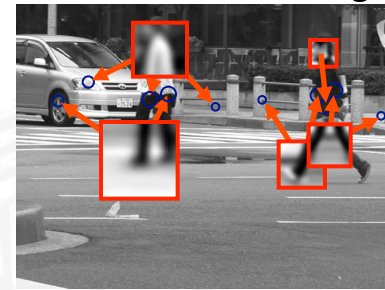
Interest Points



Matched Codebook Entries

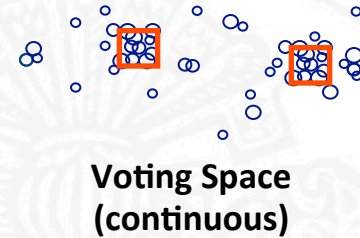


Probabilistic Voting

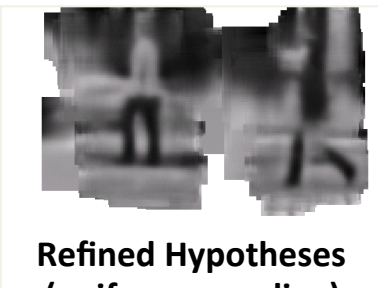


Segmentation

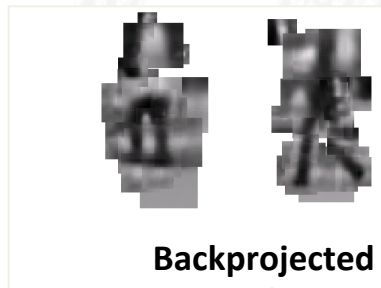
- Spatial feature configurations
- Interleaved object recognition and segmentation



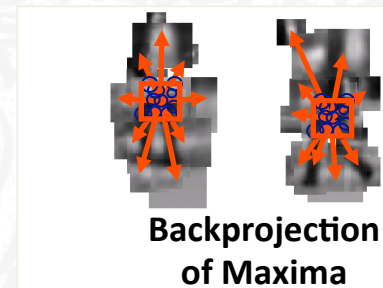
Voting Space (continuous)



Refined Hypotheses (uniform sampling)



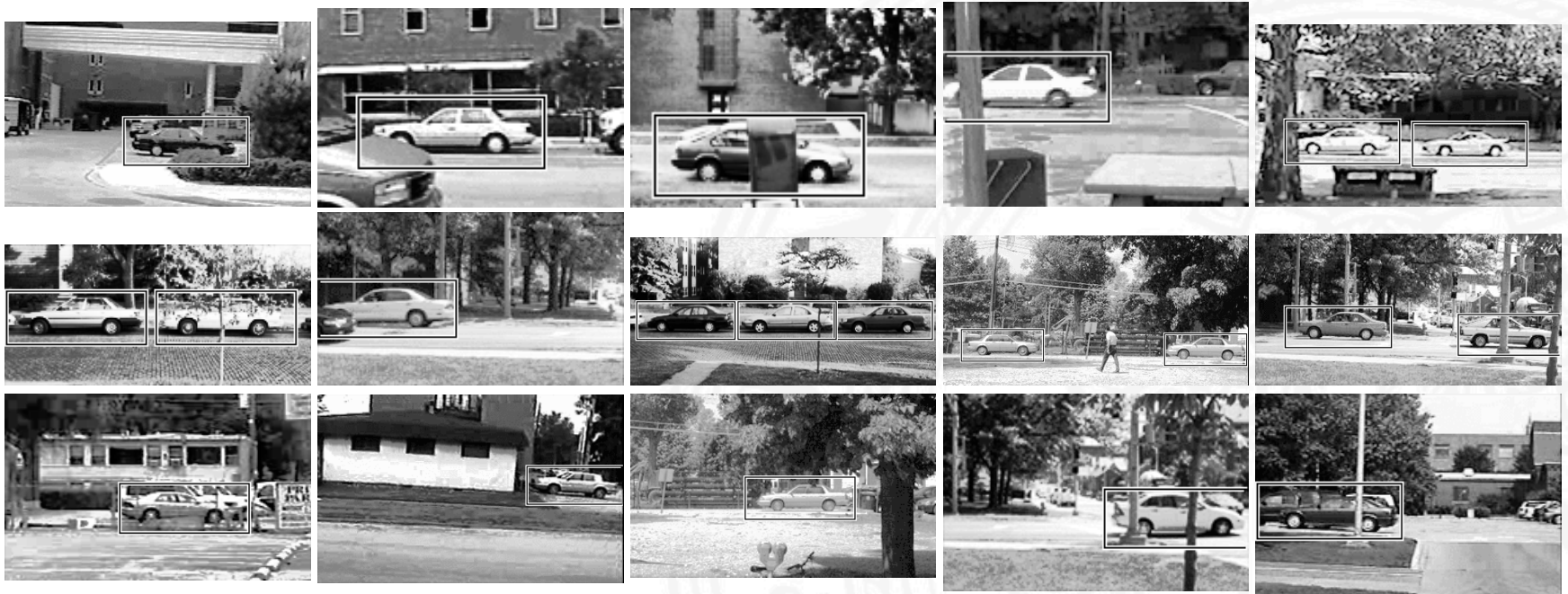
Backprojected Hypotheses



Backprojection of Maxima

# Car Detection

- Recognizes different kinds of cars
- Robust to clutter, occlusion, noise, low contrast



# Cow Detection and Segmentation

- frame-by-frame detection
- no temporal continuity exploited

