

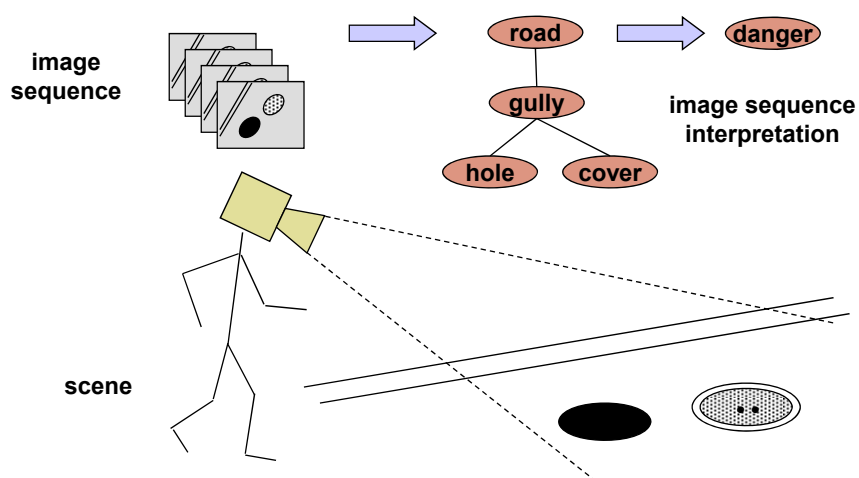
## Definition of Image Understanding

Image understanding is the task-oriented reconstruction and interpretation of a scene by means of images

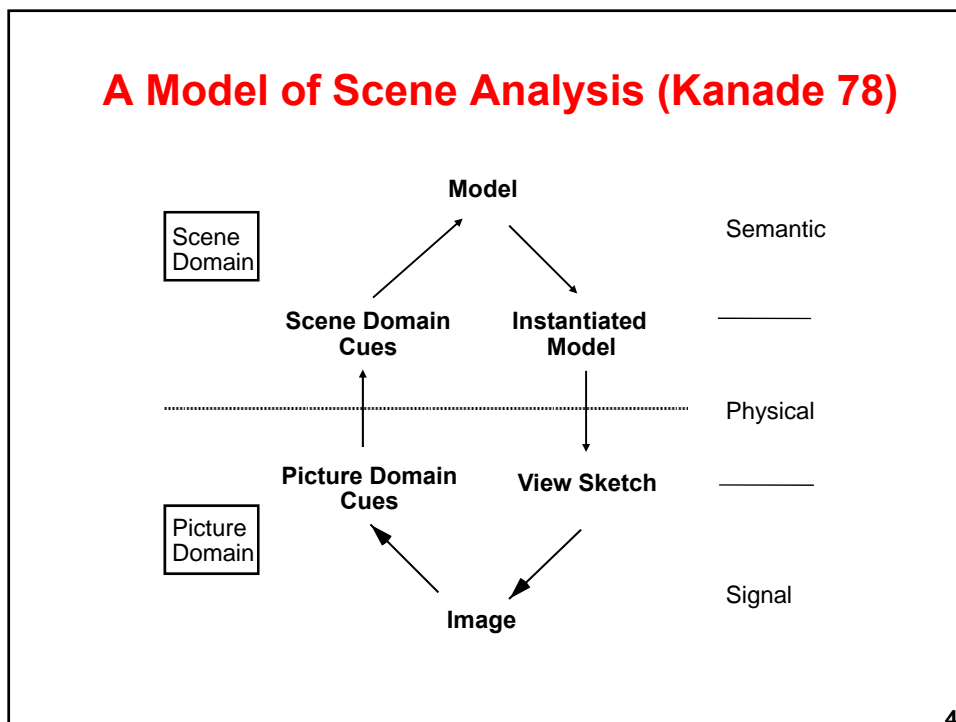
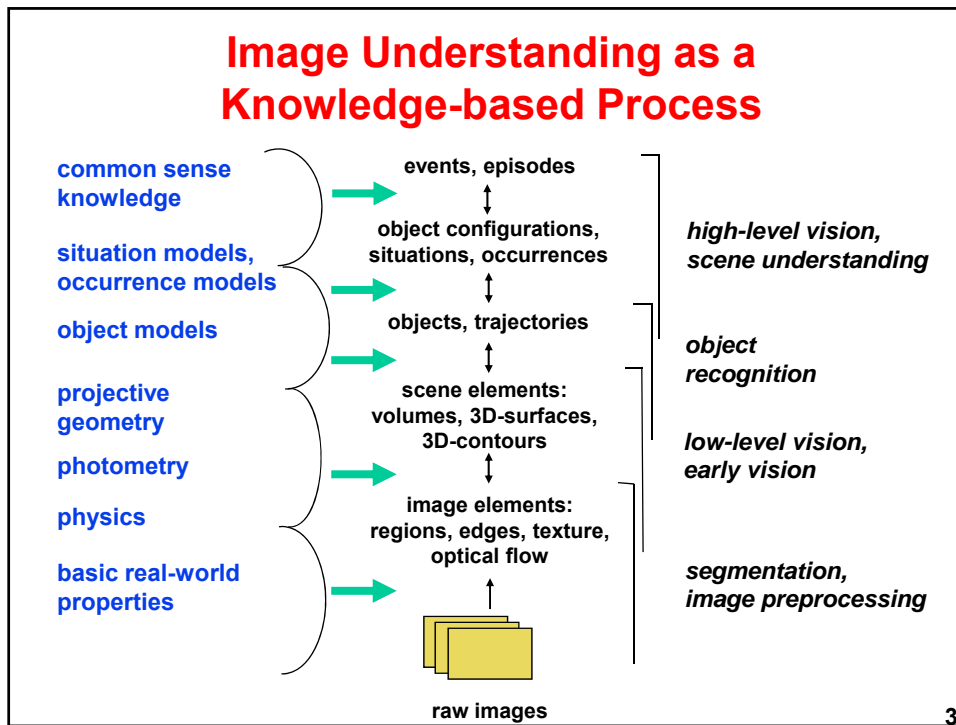
"scene":	section of the real world stationary (3D) or moving (4D)
"image":	view of a scene projection, density image (2D) depth image (2 1/2D) image sequence (3D)
"reconstruction and interpretation":	computer-internal scene description quantitative + qualitative + symbolic
"task-oriented":	for a purpose, to fulfil a particular task context-dependent, supporting actions of an agent

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## Illustration of Image Understanding



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## Abstraction Levels for the Description of Computer Vision Systems

### Knowledge level

*What knowledge or information enters a process? What knowledge or information is obtained by a process?*

*What are the laws and constraints which determine the behavior of a process?*

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### Algorithmic level

*How is the relevant information represented?*

*What algorithms are used to process the information?*

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### Implementation level

*What programming language is used?*

*What computer hardware is used?*

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## Example for Knowledge-level Analysis

*What knowledge or information enters a process? What knowledge or information is obtained by a process?*

*What are the laws and constraints which determine the behavior of a process?*

**Consider shape-from-shading:**



In order to obtain the 3D shape of an object, it is necessary to

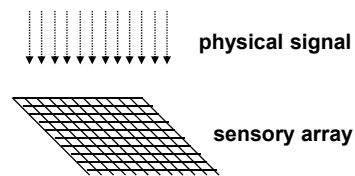
- state what knowledge is available (greyvalues, surface properties, illumination direction, etc.)
- state what information is desired (e.g. qualitative vs. quantitative)
- exploit knowledge about the physics of image formation

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## Image Formation

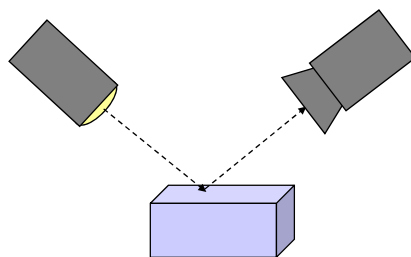
Images can be generated by various processes:

- illumination of surfaces, measurement of reflections ← "natural images"
- illumination of translucent material, measurement of irradiation
- measurement of heat (infrared) radiation
- X-ray of material, computation of density map
- measurement of any features by means of a sensory array



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## Formation of Natural Images



Intensity (brightness) of a pixel depends on

1. illumination (spectral energy, secondary illumination)
2. object surface properties (reflectivity)
3. sensor properties
4. geometry of light-source, object and sensor constellation (angles, distances)
5. transparency of irradiated medium (mistiness, dustiness)

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## Qualitative Surface Properties

When light hits a surface, it may be

- absorbed
  - reflected
  - scattered
- } in general, all effects may be mixed

Simplifying assumptions:

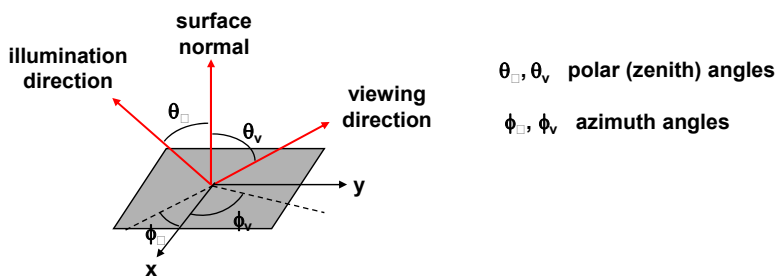
- Radiance leaving at a point is due to radiance arriving at this point
- All light leaving the surface at a wavelength is due to light arriving at the same wavelength
- Surface does not generate light internally

The "amount" of reflected light may depend on:

- the "amount" of incoming light
- the angles of the incoming light w.r.t. to the surface orientation
- the angles of the outgoing light w.r.t. to the surface orientation

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## Photometric Surface Properties



In general, the ability of a surface to reflect light is given by the Bi-directional Reflectance Distribution Function (BRDF)  $r$ :

$$r(\theta_i, \phi_i; \theta_v, \phi_v) = \frac{\delta L(\theta_v, \phi_v)}{\delta E(\theta_i, \phi_i)}$$

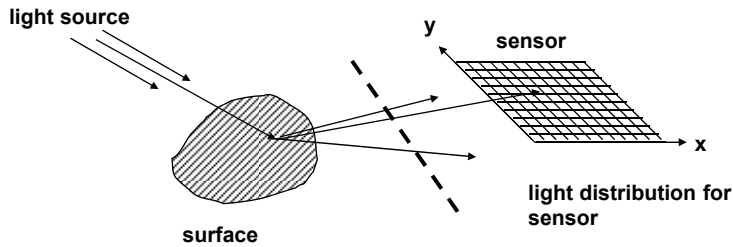
$\delta E$  = irradiance of light source received by the surface patch

$\delta L$  = radiance of surface patch towards viewer

For many materials the reflectance properties are rotation invariant, in this case the BRDF depends on  $\theta_i, \theta_v, \phi$ , where  $\phi = \phi_i - \phi_v$ .

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## Intensity of Sensor Signals



- Intensities of sensor signals depend on
- location  $x, y$  on sensor plane
  - instance of time  $t$
  - frequency of incoming light wave  $\lambda$
  - spectral sensitivity of sensor

$$f(x, y, t) = \int_0^{\infty} C(x, y, t, \lambda) S(\lambda) d\lambda$$

$\int_0^{\infty}$        $S(\lambda)$        $d\lambda$   
 spectral energy distribution      sensitivity function of sensor

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## Multispectral Images

Sensors with separate channels of different spectral sensitivities generate multispectral images:

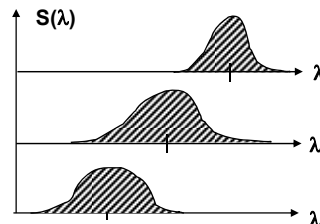
$$f_1(x, y, t) = \int_0^{\infty} C(x, y, t, \lambda) S_1(\lambda) d\lambda$$

$$f_2(x, y, t) = \int_0^{\infty} C(x, y, t, \lambda) S_2(\lambda) d\lambda$$

$$f_3(x, y, t) = \int_0^{\infty} C(x, y, t, \lambda) S_3(\lambda) d\lambda$$

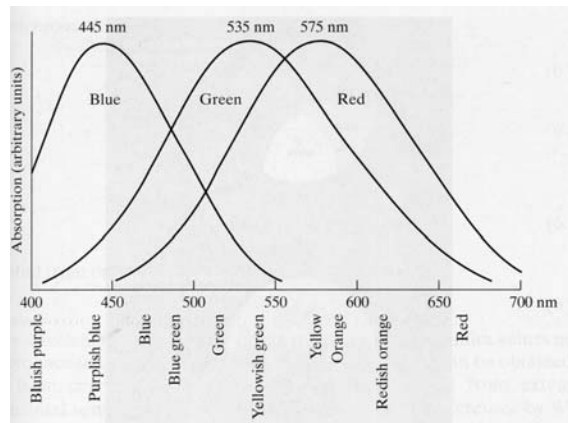
**Example:**

- R (red)      650 nm center frequency
- G (green)    530 nm center frequency
- B (blue)     410 nm center frequency



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## Spectral Sensitivity of Human Eyes



**Standardized wavelengths:**  
 red = 700 nm, green = 546.1 nm, blue = 435.8 nm

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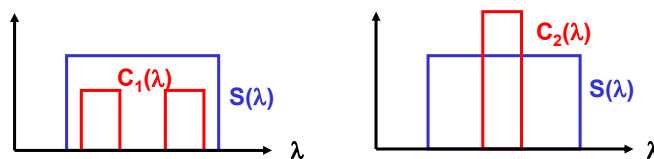
## Non-unique Sensor Response

Different spectral distributions may lead to identical sensor responses and hence cannot be distinguished

$$f(x, y, t) = \int_0^{\infty} C_1(x, y, t, \lambda) S(\lambda) d\lambda = \int_0^{\infty} C_2(x, y, t, \lambda) S(\lambda) d\lambda$$

↑
↑  
 different spectral energy distributions

**Example:**

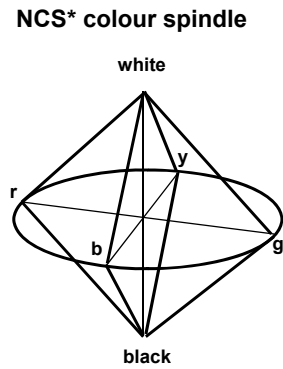
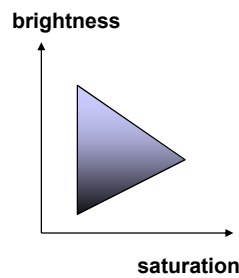
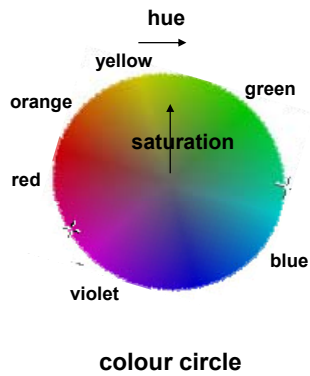


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## Dimensions of Colour

Human perception of colour distinguishes between 3 dimensions:

- hue
  - saturation
  - brightness
- } chromaticity



\* Swedish Natural Colour System

## RGB Images of a Natural Scene

Here, single colour images are rendered as greyvalue intensity images:  
stronger spectral intensity = more brightness

R+G+B

R

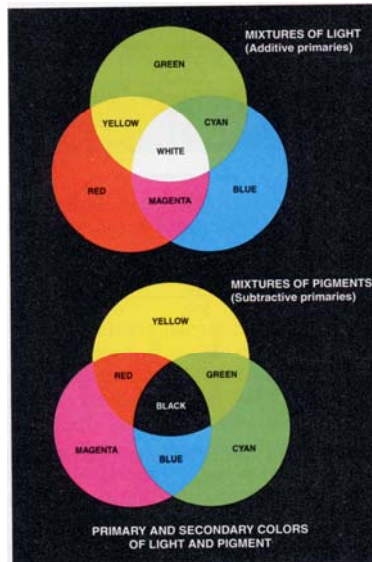
G

B





## Primary and Secondary Colours



Primary colours:

red, green, blue

Secondary colours:

magenta = red + blue

cyan = green + blue

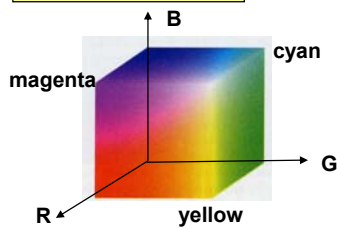
yellow = red + green

aus: Gonzales & Woods  
Digital Image Processing  
Prentice Hall 2002

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## Technical Colour Models

**RGB colour model**



Typical discretization:  
8 bits per colour dimension  
=> 16.777.216 colours

**CMY colour model**

$$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

**HSI colour model**

Hue:

$$H = \begin{cases} \Theta & \text{if } B \leq G \\ 360 - \Theta & \text{if } B > G \end{cases}$$

$$\Theta = \cos^{-1} \frac{1/2 [(R-G) + (R-B)]}{[(R-G)^2 + (R-B)(G-B)]^{1/2}}$$

Saturation:

$$S = 1 - \frac{3}{(R + G + B)} [\min(R, G, B)]$$

Intensity:

$$I = 1/3 (R + G + B)$$

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## Discretization of Images

Image functions must be discretized for computer processing:

- **spatial quantization**  
the image plane is represented by a 2D array of picture cells
- **greyvalue quantization**  
each greyvalue is taken from a discrete value range
- **temporal quantization**  
greyvalues are taken at discrete time intervals

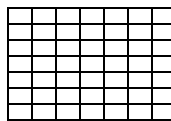
$$f(x,y,t) \Rightarrow \{ f_s(x_1, y_1, t_1), f_s(x_2, y_2, t_1), f_s(x_3, y_3, t_1), \dots \\ f_s(x_1, y_1, t_2), f_s(x_2, y_2, t_2), f_s(x_3, y_3, t_2), \dots \\ f_s(x_1, y_1, t_3), f_s(x_2, y_2, t_3), f_s(x_3, y_3, t_3), \dots \}$$

A single value of the discretized image function is called a pixel (picture element).

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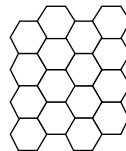
## Spatial Quantization

Rectangular grid



Greyvalues represent the quantized value of the signal power falling into a grid cell.

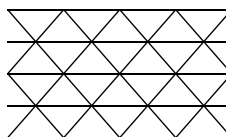
Hexagonal grid



Note that samples of a hexagonal grid are equally spaced along rows, with successive rows shifted by half a sampling interval.



Triangular grid

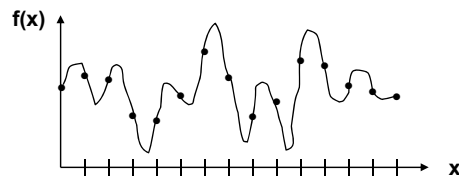


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## Reconstruction from Samples

Under what conditions can the original (continuous) signal be reconstructed from its sampled version?

Consider a 1-dimensional function  $f(x)$ :



Reconstruction is only possible, if "variability" of function is restricted.

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## Sampling Theorem

**Shannon's Sampling Theorem:**

A bandlimited function with bandwidth  $W$  can be exactly reconstructed from equally spaced samples, if the sampling distance is not larger than  $\frac{1}{2W}$

bandwidth = largest frequency contained in signal

(=> Fourier decomposition of a signal)

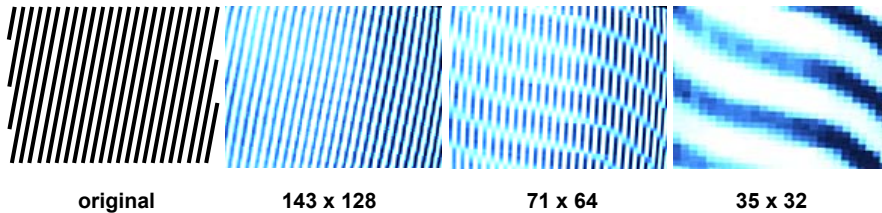
Analogous theorem holds for 2D signals with limited spatial frequencies  $W_x$  and  $W_y$

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## Aliasing

Sampling an image with fewer samples than required by the sampling theorem may cause "aliasing" (artificial structures).

Example:



To avoid aliasing, bandwidth of image must be reduced prior to sampling.  
(=> low-pass filtering)

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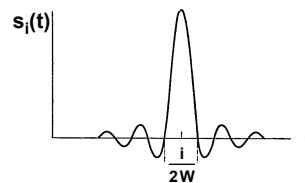
## Reconstructing the Image Function from Samples

Formally, a continuous function  $f(t)$  with bandwidth  $W$  can be exactly reconstructed using sampling functions  $s_i(t)$ :

$$s_i(t) = \sqrt{2W} \frac{\sin 2\pi W [t - i / (2W)]}{2\pi W [t - i / (2W)]}$$

$$x(t) = \sum_{i=-\infty}^{\infty} \underbrace{\sqrt{\frac{1}{2W}} x\left(\frac{i}{2W}\right)}_{\text{sample values}} S_i(t)$$

sample values



An analogous equation holds for 2D.

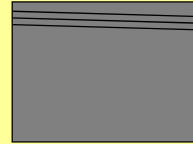
In practice, image functions are generated from samples by interpolation.

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## Sampling TV Signals

### PAL standard:

- picture format 3 : 4
- 25 full frames (50 half frames) per second
- interlaced rows: 1, 3, 5, ... , 2, 4, 6, ...
- 625 rows per full frame, 576 visible
- 64  $\mu$ s per row, 52  $\mu$ s visible
- 5 MHz bandwidth



Only 1D sampling is required because of fixed row structure.

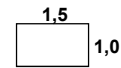
Sampling intervals of  $\Delta t = 1/(2W) = 10^{-7}$  s = 100 ns give maximal possible resolution.

With  $\Delta t = 100$  ns, a row of duration 52  $\mu$ s gives rise to 520 samples.

In practice, one often chooses 512 pixels per TV row.

=> 576 x 512 = 294912 pixels per full frame

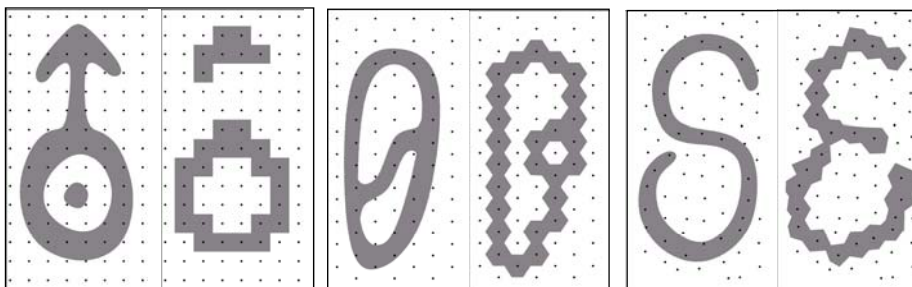
=> rectangular pixel size with width/height =  $(\frac{4}{512}) / (\frac{3}{576}) = 1,5$



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## Sampling of Binary Images (1)

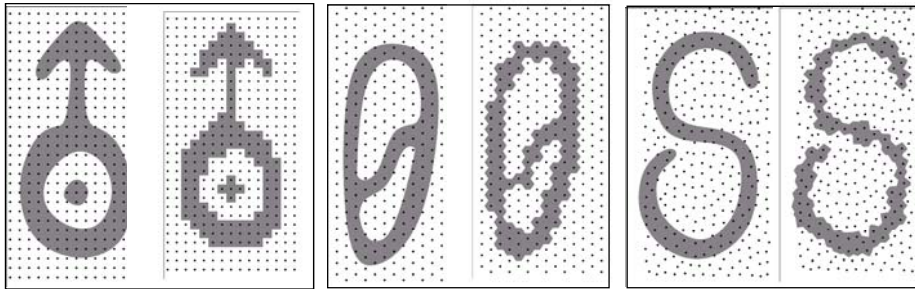
Problem: Shapes may change under digitization



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## Sampling of Binary Images (2)

**Problem: Shapes may change under digitization**



This cannot be solved by using Shannon's Theorem since binary images are not bandlimited.

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## Shape Preserving Sampling Theorem (1)

**Shape Preserving Sampling Theorem:**

The shape of an  $r$ -regular image can be correctly reconstructed after sampling with any sampling grid, if the grid point distance is not larger than  $r$ .

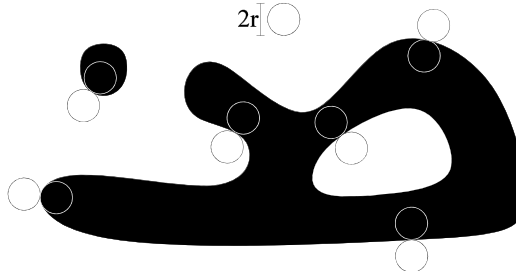
Steldinger, Köthe 2003

"grid point distance": maximal distance from arbitrary sampling point to the next sampling point

" $r$ -regular binary image":

osculating  $r$ -discs at each boundary point of the shape

- ⇒ curvature bounded by  $1/r$
- ⇒ bounded thinness of parts
- ⇒ minimal distance between parts



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## Shape Preserving Sampling Theorem (2)

What does correct reconstruction mean?

Topological and geometric similarity criterion:

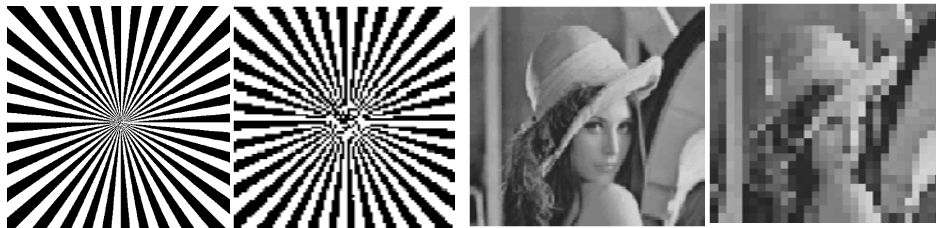
One shape can be mapped onto the other by twisting the whole plane, such that the displacement of each point is smaller than  $r$ .

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## Sampling of Shapes in Arbitrary Images (1)

The previous sampling theorem also holds for greyvalue images, if each level set is an  $r$ -regular shape.

A "level set" is the set where the image is brighter than a given threshold value.

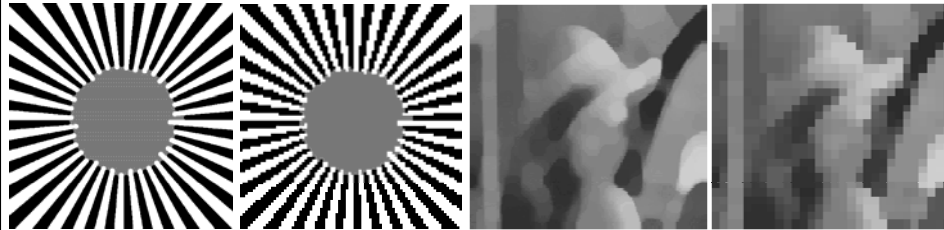


sampling + reconstruction

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## Sampling of Shapes in Arbitrary Images (2)

Reconstruction after sampling from r-regular originals



There exist generalizations to more complex cases (e.g. higher dimensions, blurring, colors, noise).

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## Comparison of the Sampling Theorems

	Shannon's Sampling Theorem	Shape Preserving Sampling Theorem
necessary image property	bandlimited with bandwidth $W$	r-regular
equation	$\left(\frac{r'}{\sqrt{2}} = d\right) \quad d < \frac{1}{2W}$	$r' < r$
reconstructed image	identical to original image	same shape as the original image
prefiltering	band-limitation: efficient algorithms (but shapes may change!)	regularization: unsolved problem
2D sampling grid	rectangular grid	arbitrary grids
dimension of definition	1D (generalizable to n-D)	2D (partly generalizable to n-D)

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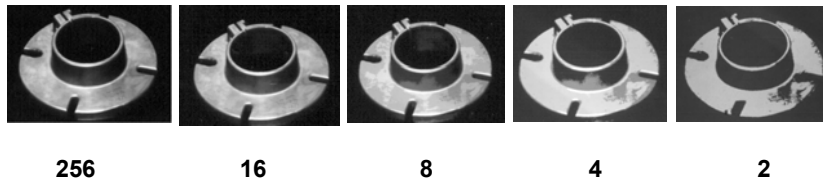
## Quantization of Greyvalues

Quantization of greyvalues transforms continuous values of a sampled image function into digital quantities.

Typically  $2 \dots 2^{10}$  quantization levels are used, depending on task.

Less than  $2^9$  quantization levels may cause artificial contours for human perception.

Example:

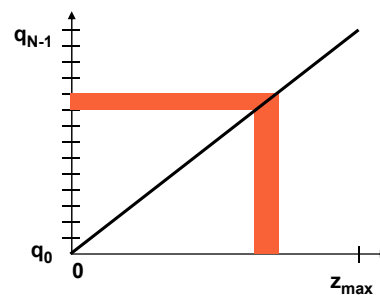


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## Uniform Quantization

Equally spaced discrete values  $q_0 \dots q_{N-1}$  represent equal-width greyvalue intervals of the continuous signal.

Typically  $N = 2^K$  for  $K = 1 \dots 10$



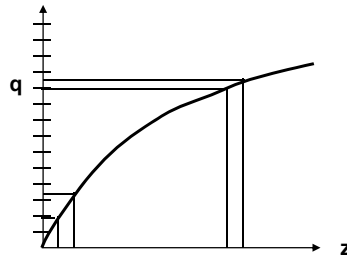
Uniform quantization may "waste" quantization levels, if greyvalues are not equally distributed.

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## Nonlinear Quantization Curves

E.g. fine resolution for "interesting" greyvalue ranges, coarse resolution for less interesting greyvalue ranges.

**Example:**  
Low greyvalues are mapped into more quantization levels than high greyvalues.



**Note:**

Subjective brightness in human perception depends (roughly) logarithmically on the actual (measurable) brightness.

To let the computer see brightness as humans, use a logarithmic quantization curve.

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## Optimal Quantization (1)

**Assumption:**

Probability density  $p(z)$  for continuous greyvalues and number of quantization levels  $N$  are known.

**Goal:**

Minimize mean quadratic quantization error  $d_q$  by choosing optimal interval boundaries  $z_n$  and optimal discrete representatives  $q_n$ .

$$d_q^2 = \sum_{n=0}^{N-1} \int_{z_n}^{z_{n+1}} (z - q_n)^2 p(z) dz$$

Minimizing by setting the derivatives zero:

$$\frac{\delta}{\delta z_n} d_q^2 = (z_n - q_{n-1})^2 p(z_n) - (z_n - q_n)^2 p(z_n) = 0 \quad \text{for } n = 1 \dots N-1$$

$$\frac{\delta}{\delta q_n} d_q^2 = -2 \int_{z_n}^{z_{n+1}} (z - q_n) p(z) dz = 0 \quad \text{for } n = 0 \dots N-1$$

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## Optimal Quantization (2)

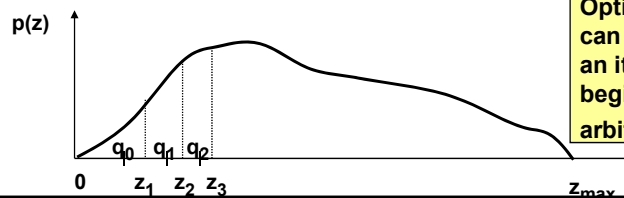
Solution for optimal quantization:

$$z_n = \frac{1}{2} (q_{n-1} + q_n) \quad \text{for } n = 1 \dots N - 1 \text{ when } p(z_n) > 0$$

Each interval boundary must be in the middle of the corresponding quantization levels.

$$q_n = \frac{\int_{z_n}^{z_{n+1}} zp(z) dz}{\int_{z_n}^{z_{n+1}} p(z) dz} \quad \text{for } n = 0 \dots N - 1$$

Each quantization level is the center-of-gravity coordinate of the corresponding probability density area.



Optimal quantization can be determined by an iterative algorithm beginning with an arbitrary choice of  $z_1$

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## Binarization

For many applications it is convenient to distinguish only between 2 greyvalues, "black" and "white", or "1" and "0".

Example: Separate object from background

**Binarization = transforming an image function into a binary image**

Thresholding:

$$g(x, y) \Rightarrow \begin{cases} 0 & \text{if } g(x, y) < T \\ 1 & \text{if } g(x, y) \geq T \end{cases} \quad T \text{ is threshold}$$

Thresholding is often applied to digital images in order to isolate parts of the image, e.g. edge areas.

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## Threshold Selection by Trial and Error

A threshold which perfectly isolates an image component must not always exist.

Selection by trial and error:

Select threshold until some image property is fulfilled, e.g.

$$q = \frac{\# \text{ white pixels}}{\# \text{ black pixels}} \Rightarrow q_0$$

line strength  $\Rightarrow d_0$

number of connected components  $\Rightarrow n_0$

Number of trials may be small if logarithmic search can be used.

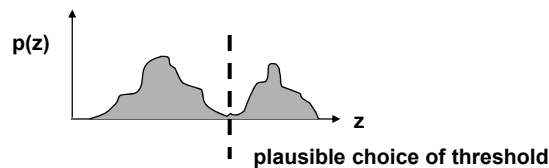
Example:

At most 8 trials are needed to select a threshold  $0 \leq T \leq 255$  which best approximates a given  $q_0$ .

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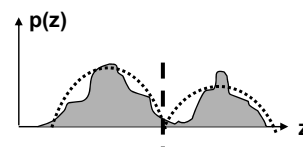
## Distribution-based Threshold Selection

The greyvalue distribution of the image function may show a bimodality:

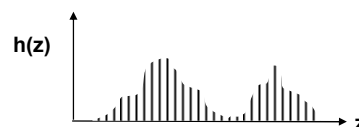


Two methods for finding a plausible threshold:

1. Find "valley" between two "hills"
2. Fit hill templates and compute intersection



Typically, computations are based on histograms which provide a discrete approximation of a distribution.

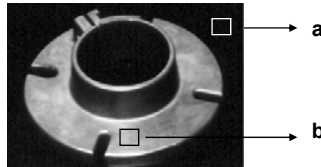


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## Threshold Selection Based on Reference Positions

In many applications, the approximate position of image components is known a priori. These positions may provide useful reference greyvalues.

**Example:**



possible choice of threshold:

$$T = \frac{a+b}{2}$$

Threshold selection and binarization may be decisively facilitated by a good choice of illumination and image capturing techniques.

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## Image Capturing for Thresholding

If the image capturing process can be controlled, thresholding can be facilitated by a suitable choice of

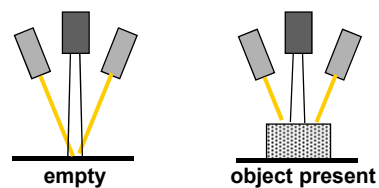
- illumination
- camera position
- object placement
- background greyvalue or colour
- preprocessing

**Example: Backlighting**

Illumination from the rear gives bright background and shadowed object

**Example: Slit illumination**

On a conveyor belt illuminated by a light slit at an angle, elevations give rise to displacements which can be recognized by a camera.



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