

Perspective and Orthographic Projection

Within the camera coordinate system the <u>perspective projection</u> of a scene point onto the image plane is described by

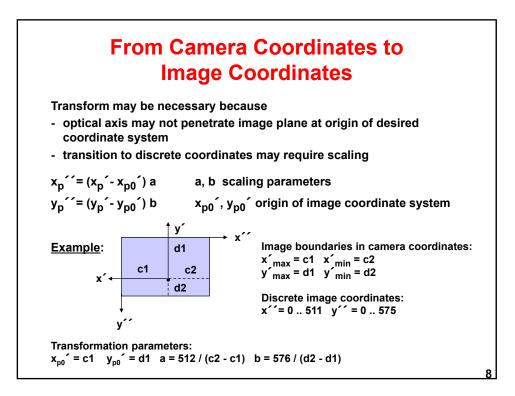
$$x_{p}' = \frac{x'f}{z'}$$
 $y_{p}' = \frac{y'f}{z'}$ $z_{p}' = f$ (f = focal distance)

- nonlinear transformation
- loss of information

If all objects are far away (large z´), f/z´ is approximately constant => <u>orthographic projection</u>

 $x_p = s x y_p = s y$ (s = scaling factor)

Orthographic projection can be viewed as projection with parallel rays + scaling



Complete Perspective Projection Equation

We combine the 3 transformation steps:

1. scene coordinates => camera coordinates

- 2. projection of camera coordinates into image plane
- 3. camera coordinates => image coordinates

$$\begin{split} x_p^{\prime \prime} &= \{ f/z^{\prime} [\cos \beta \cos \gamma \ (x - x_0) + \cos \beta \sin \gamma \ (y - y_0) + \sin \beta \ (z - z_0)] - x_{p0} \} a \\ y_p^{\prime \prime} &= \{ f/z^{\prime} [(-\sin \alpha \sin \beta \cos \gamma - \cos \alpha \sin \gamma) \ (x - x_0) + \\ (-\sin \alpha \sin \beta \sin \gamma + \cos \alpha \cos \gamma) \ (y - y_0) + \\ \sin \alpha \cos \beta \ (z - z_0)] - y_{p0} \} b \\ \\ \text{with } z^{\prime} &= (-\cos \alpha \sin \beta \cos \gamma + \sin \alpha \sin \gamma) \ (x - x_0) + \\ (-\cos \alpha \sin \beta \sin \gamma - \sin \alpha \cos \gamma) \ (y - y_0) + \\ \cos \alpha \cos \beta \ (z - z_0) \end{split}$$

