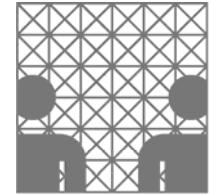


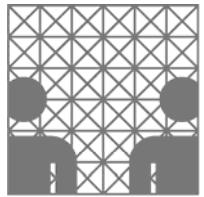


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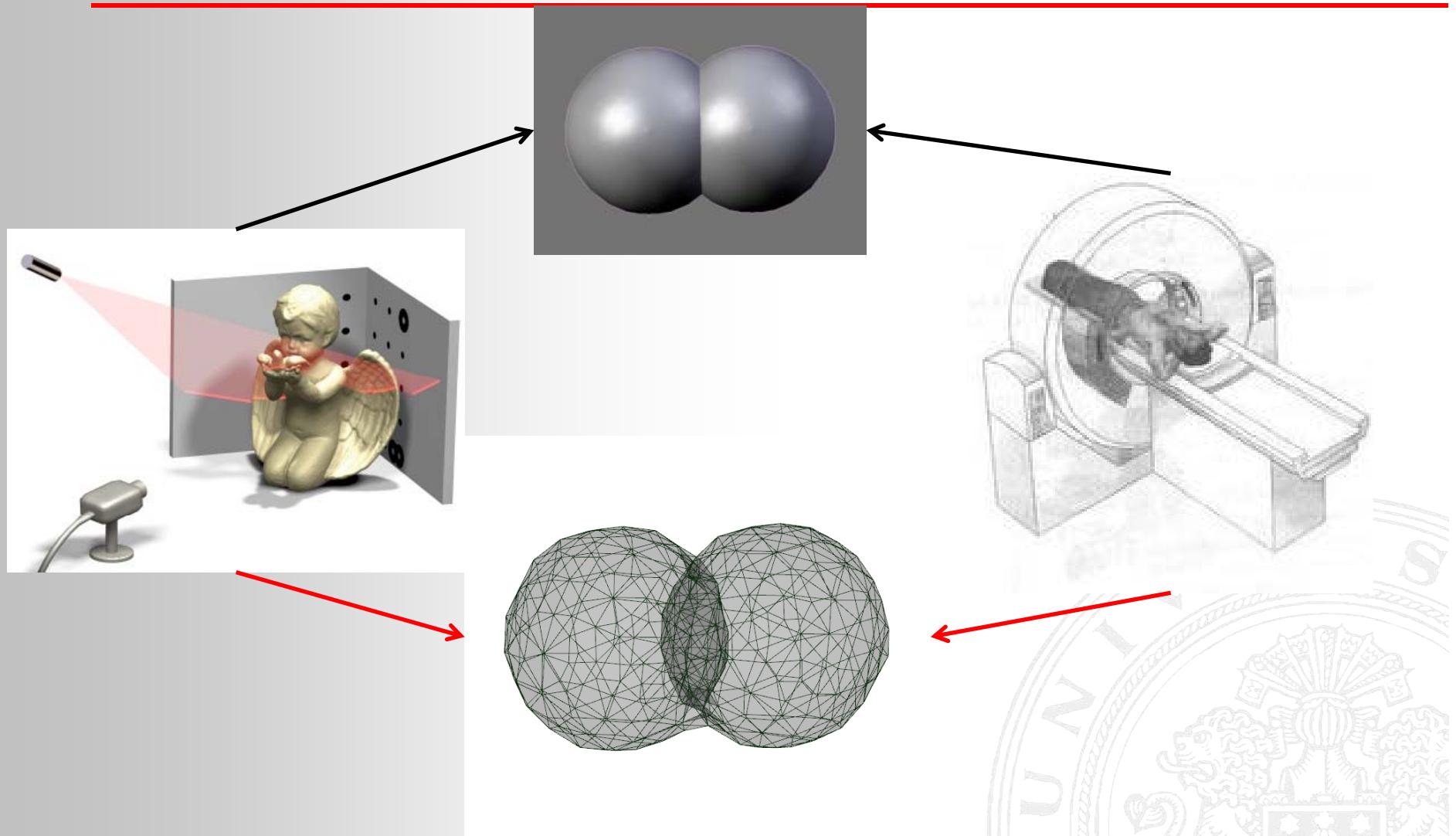
Seminar WS 08/09
Surface Reconstruction
Dr. Peer Stelldinger



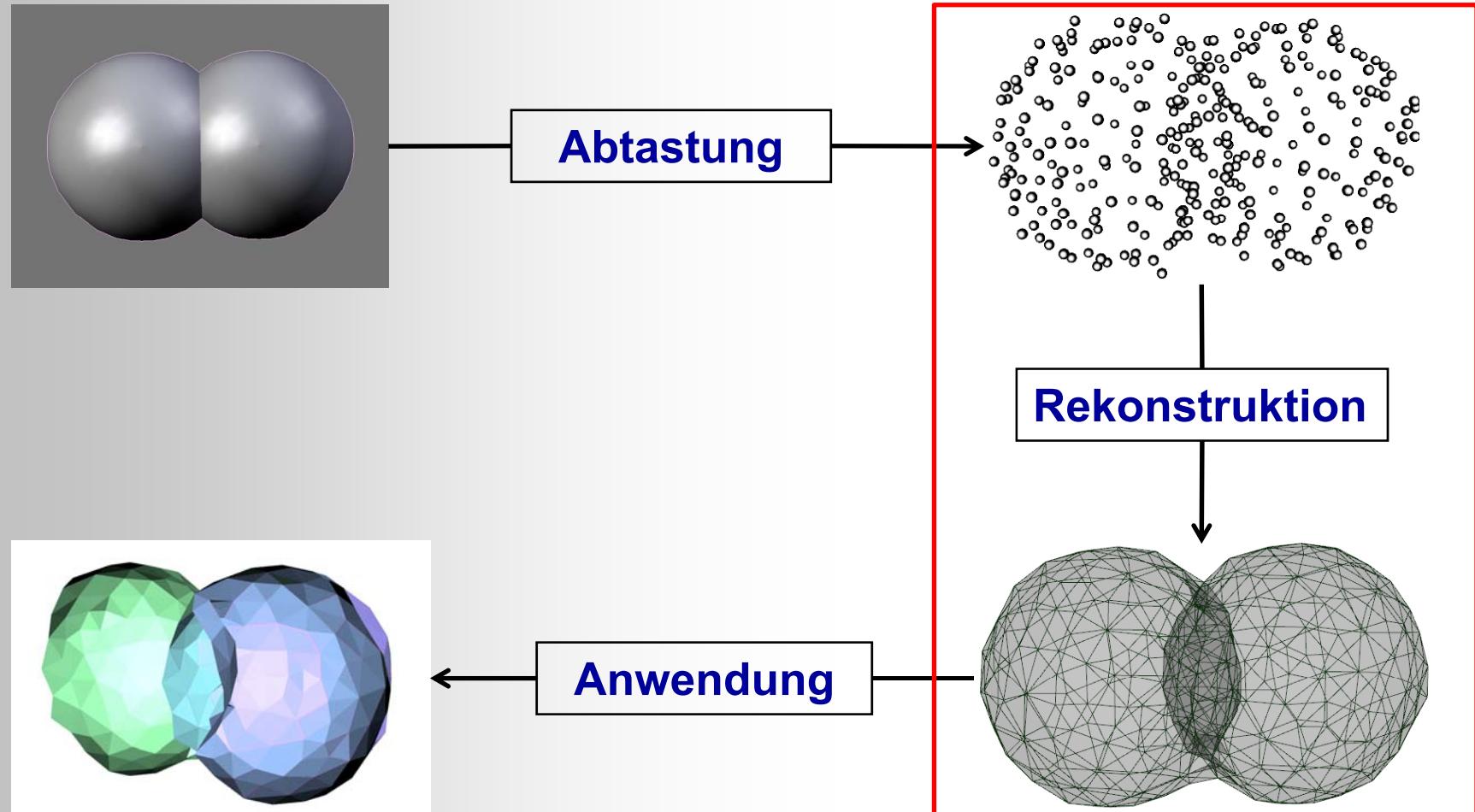
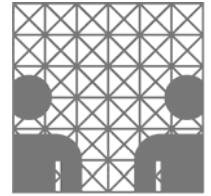
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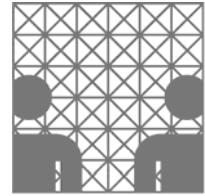
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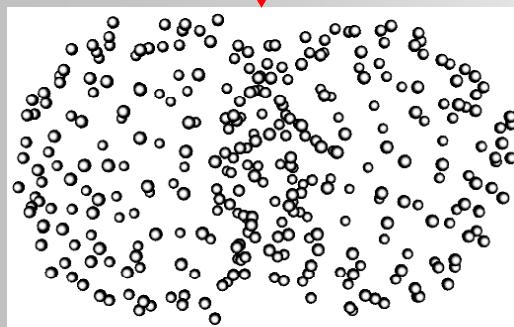
Digitalisierung



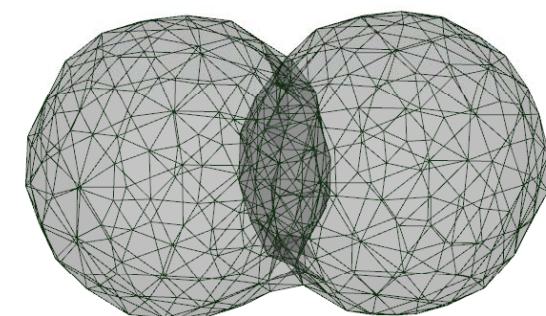
Rekonstruktion



Bedienungen an die Abtastung

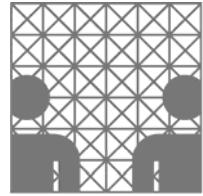


Beweisverfahren

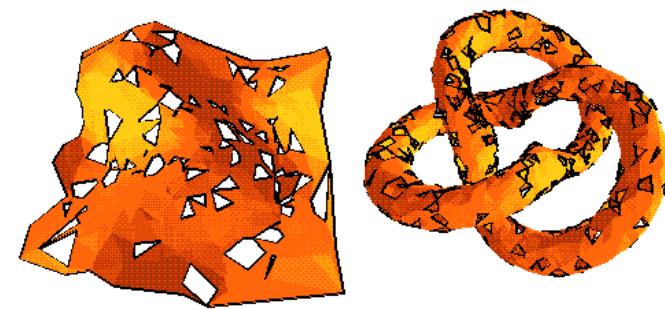
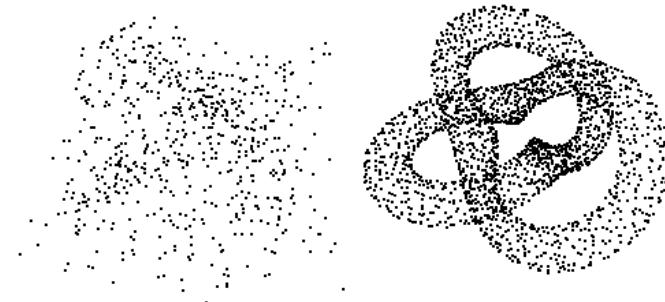


Methode

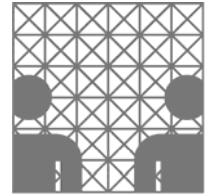
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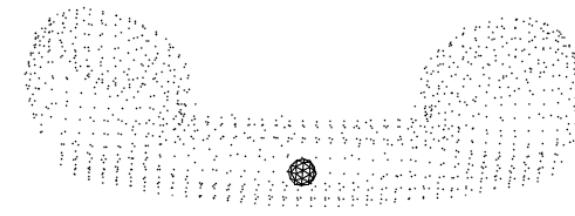
- Computational Geometry



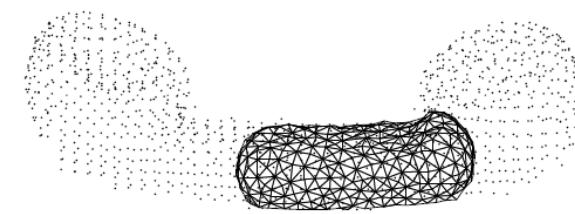
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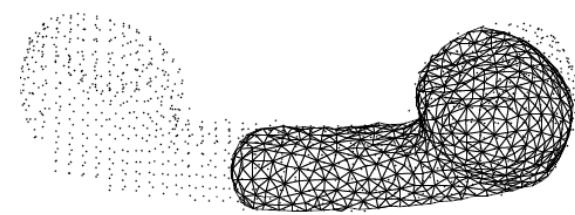
- Computational Geometry
- Surface Fitting



(a)



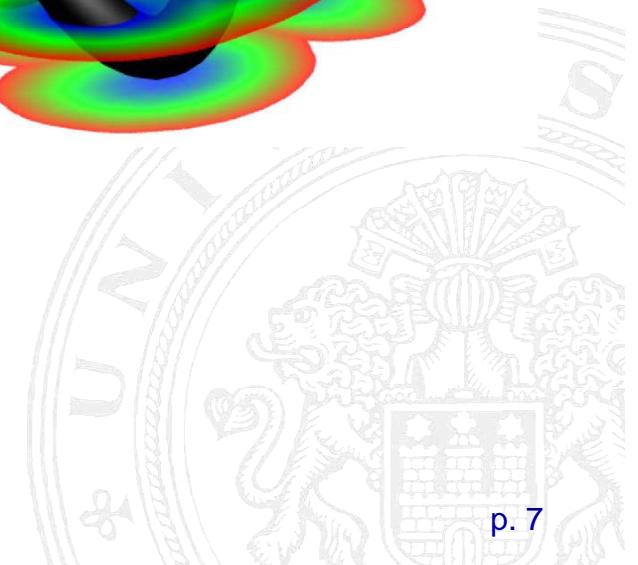
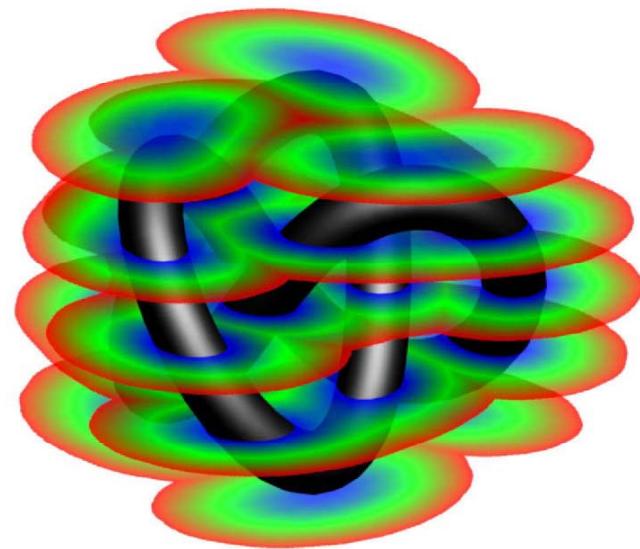
(c)



Surface Reconstruction



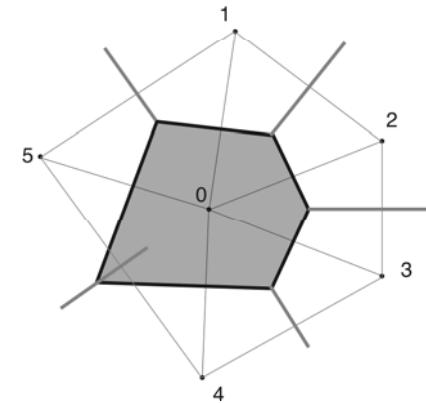
- Computational Geometry
- Surface Fitting
- Implicit Function Fitting



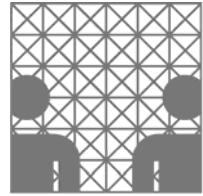
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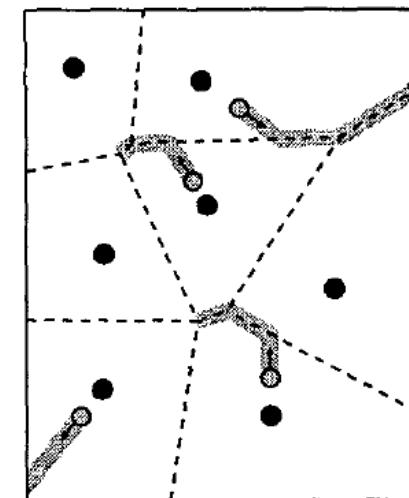
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes



Computational Geometry



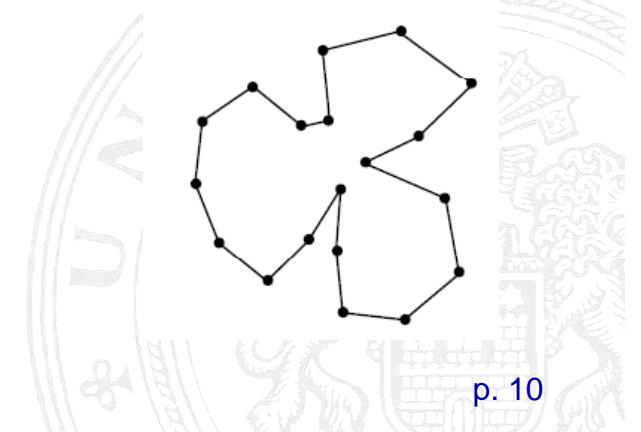
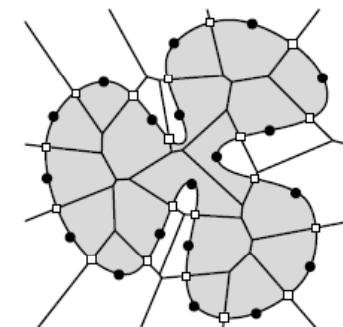
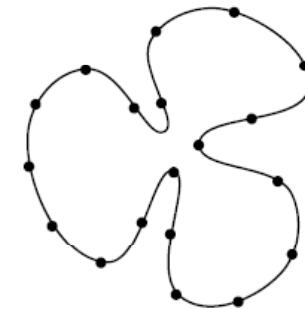
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes



Computational Geometry



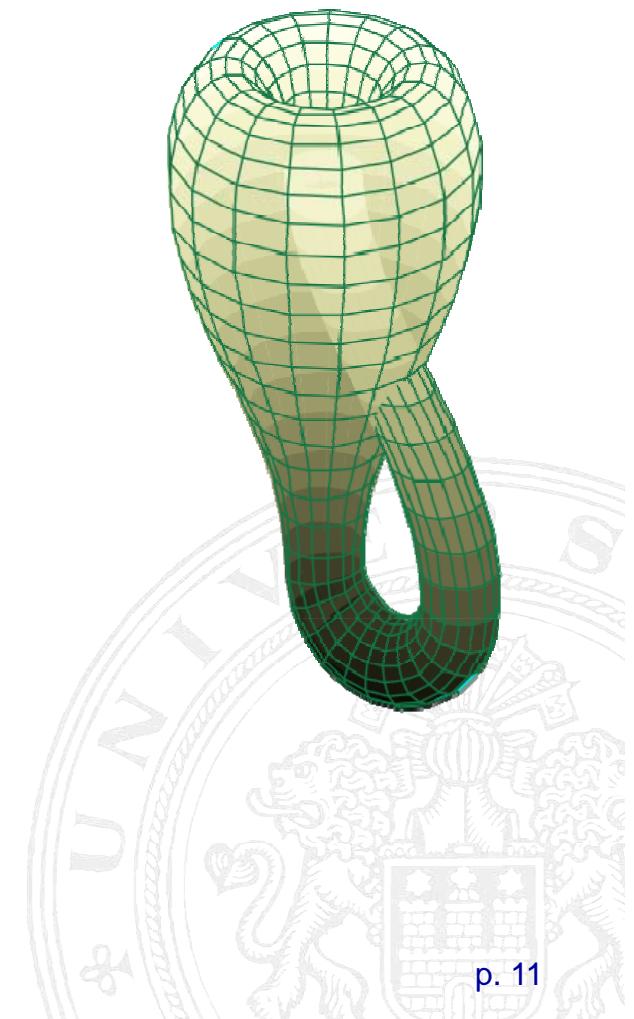
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction



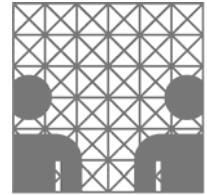
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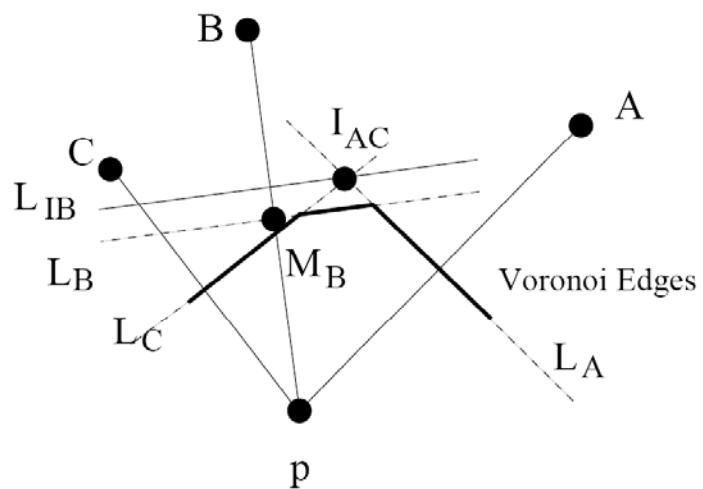
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time



Computational Geometry



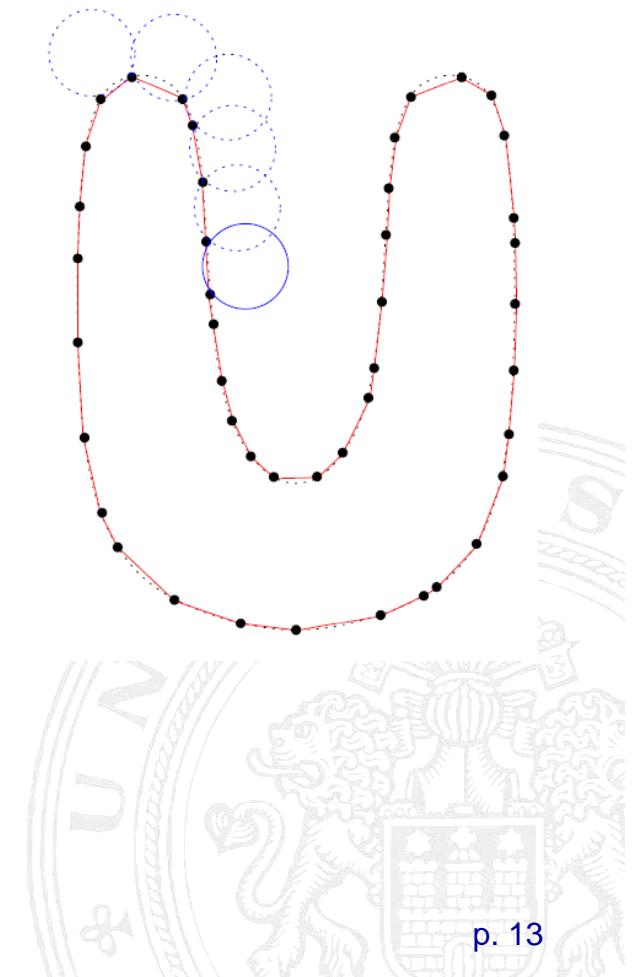
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
 - Flow Shapes
 - r-Regular Shape Reconstruction
 - One Triangle at a Time
 - Lower Dimensional Localized Delaunay Triangulation



Computational Geometry



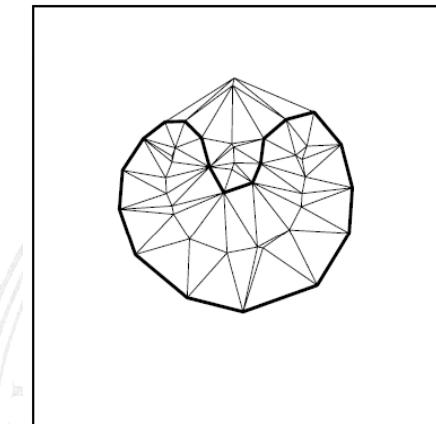
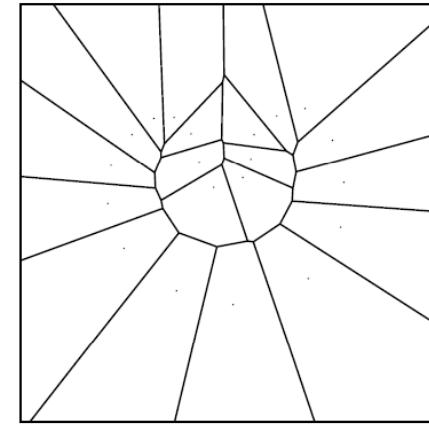
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting



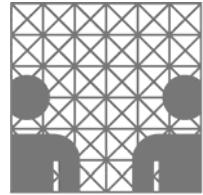
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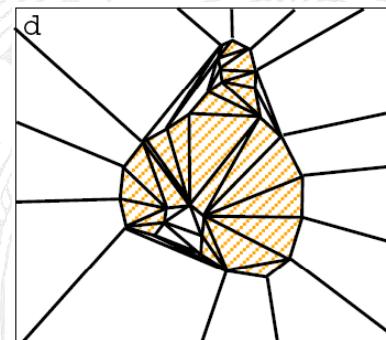
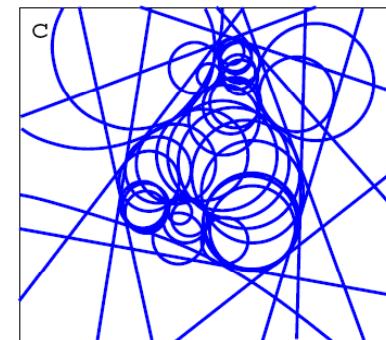
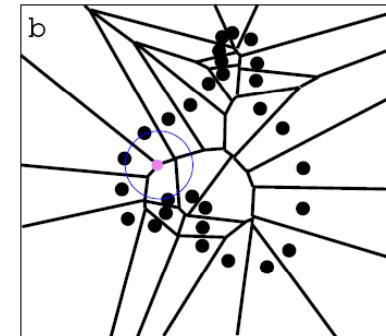
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust



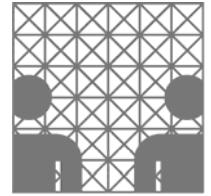
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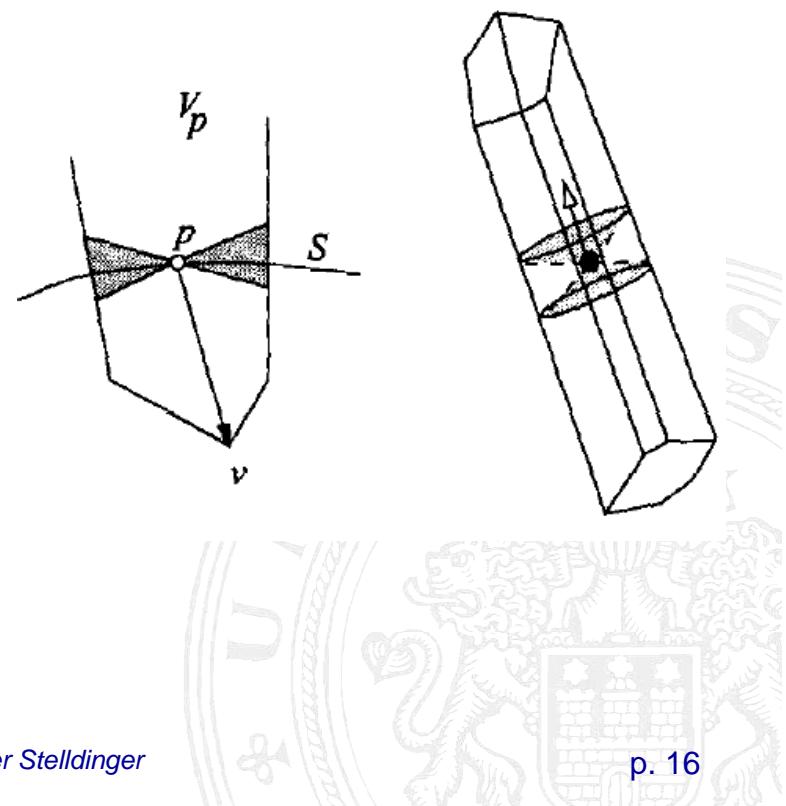
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust
- Power Crust



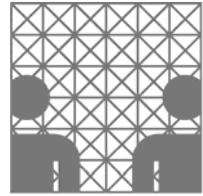
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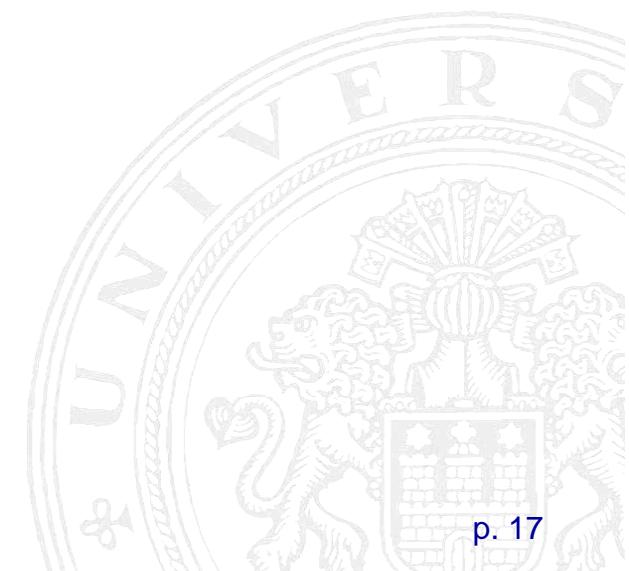
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust
- Power Crust
- Cocone



Computational Geometry



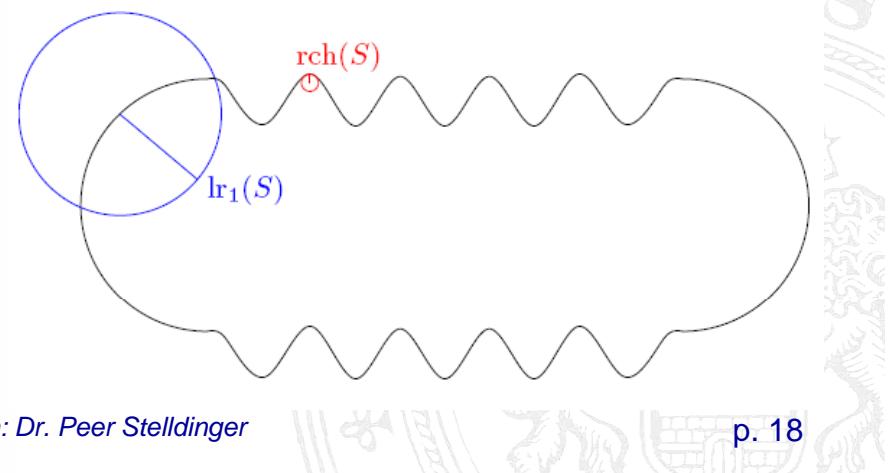
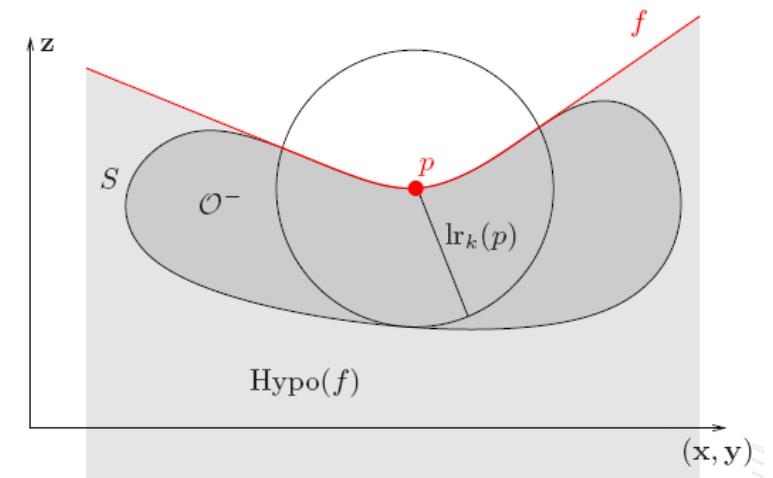
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust
- Power Crust
- Cocone
- Homology of Submanifolds



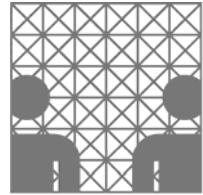
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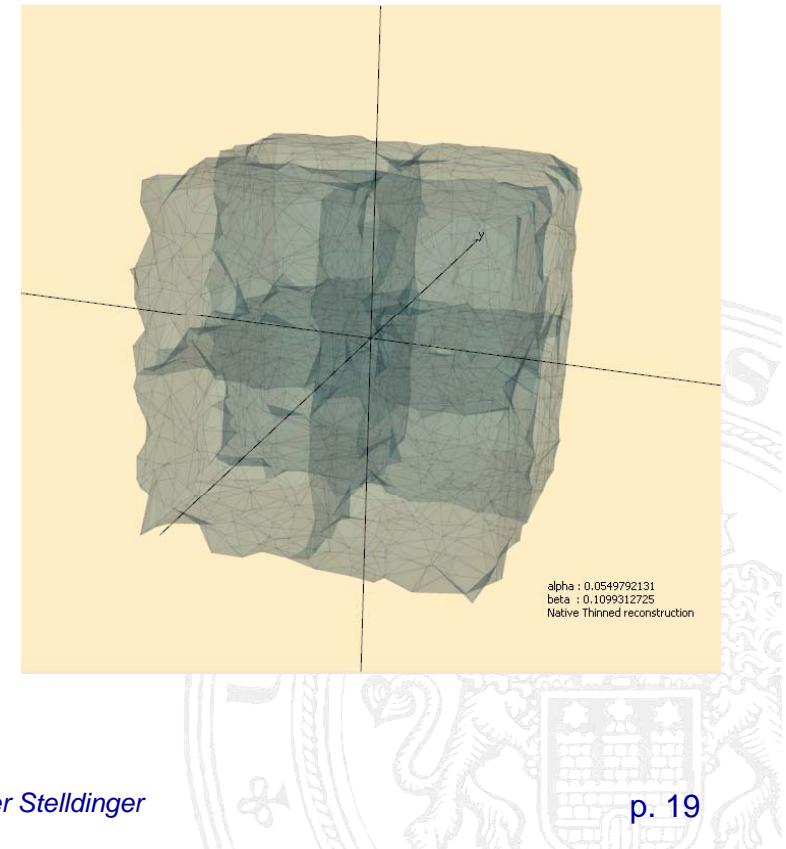
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust
- Power Crust
- Cocone
- Homology of Submanifolds
- Lipschitz Surfaces



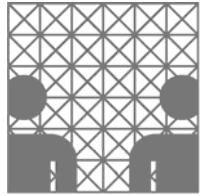
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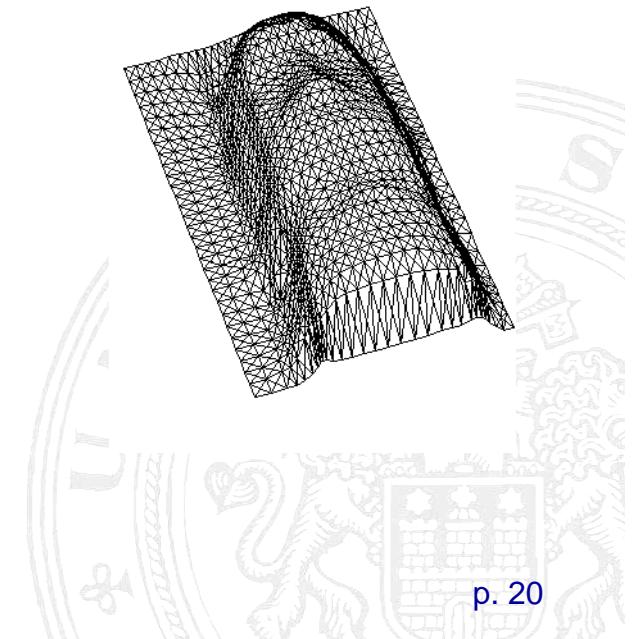
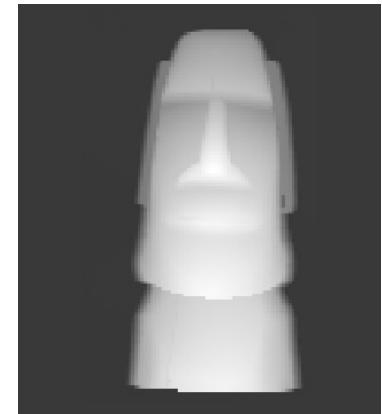
- Voronoi Diagrams, Delaunay Triangulations and Alpha Shapes
- Flow Shapes
- r-Regular Shape Reconstruction
- One Triangle at a Time
- Lower Dimensional Localized Delaunay Triangulation
- Ball Pivoting
- Crust
- Power Crust
- Cocone
- Homology of Submanifolds
- Lipschitz Surfaces
- r-Stable Reconstruction



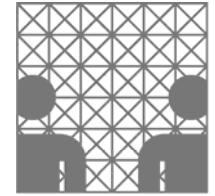
Surface Fitting



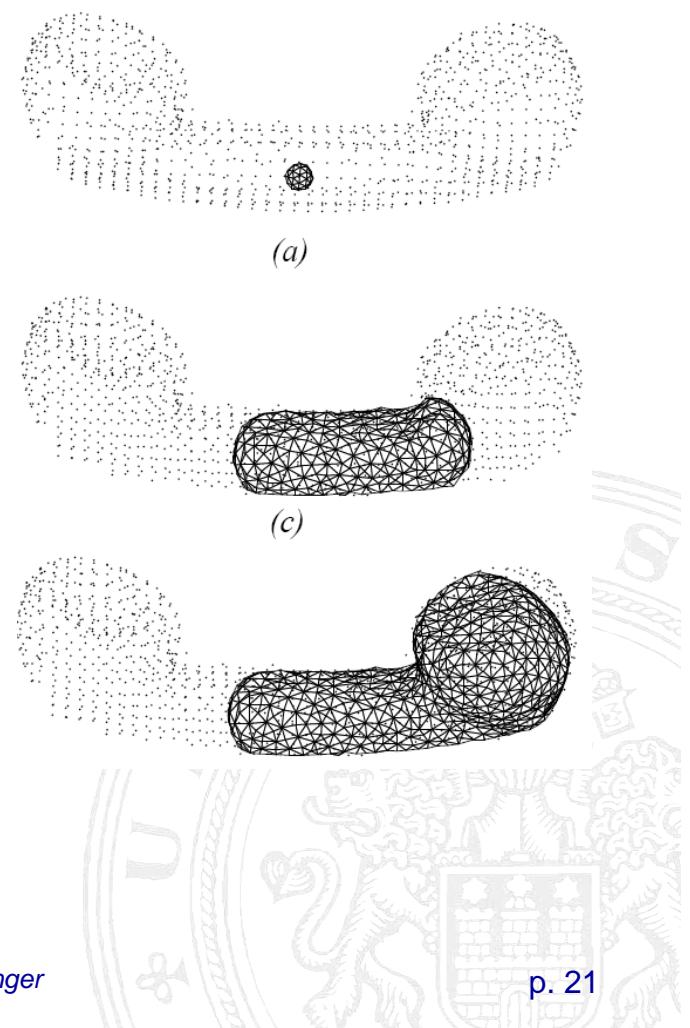
- Adaptive Meshes



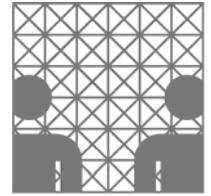
Surface Fitting



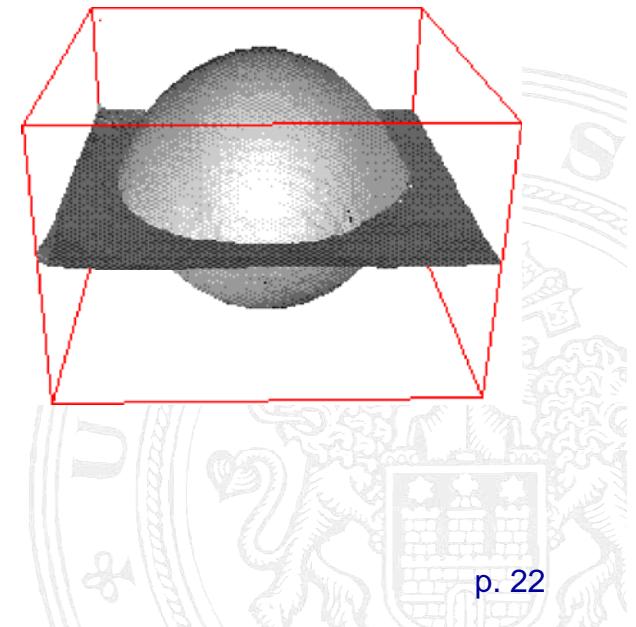
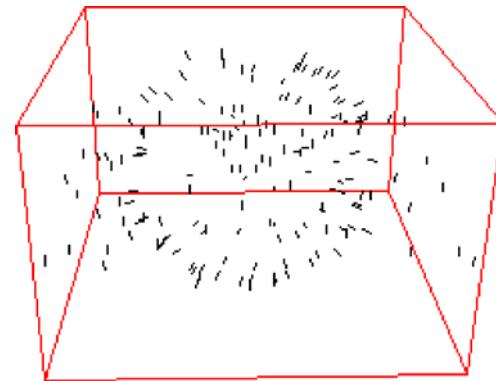
- Adaptive Meshes
- Balloon Fitting



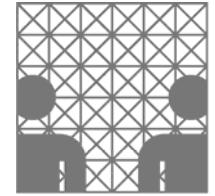
Surface Fitting



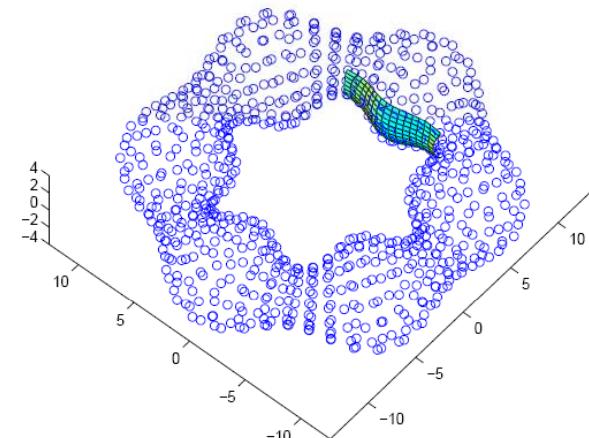
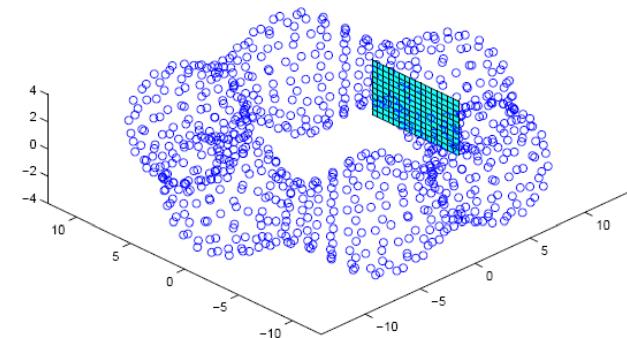
- Adaptive Meshes
- Balloon Fitting
- Surface Inferencing



Surface Fitting



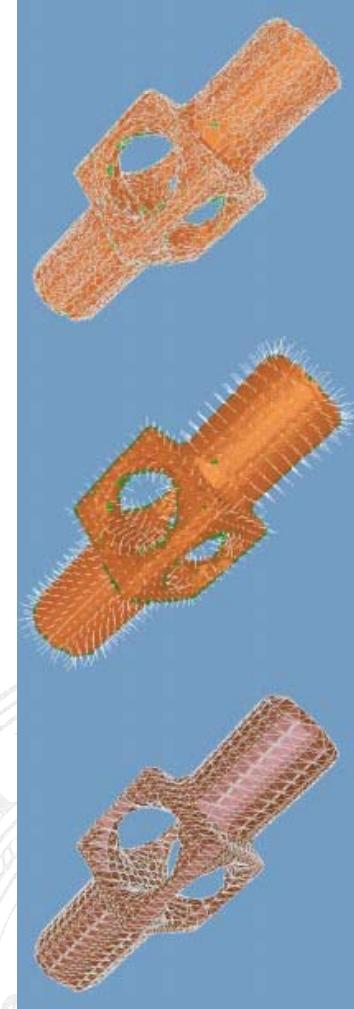
- Adaptive Meshes
- Balloon Fitting
- Surface Inferencing
- Moving Least Squares



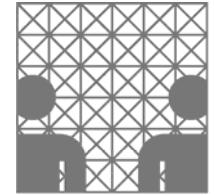
Implicit Function Fitting



- Surfaces from Unorganized Points



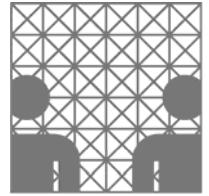
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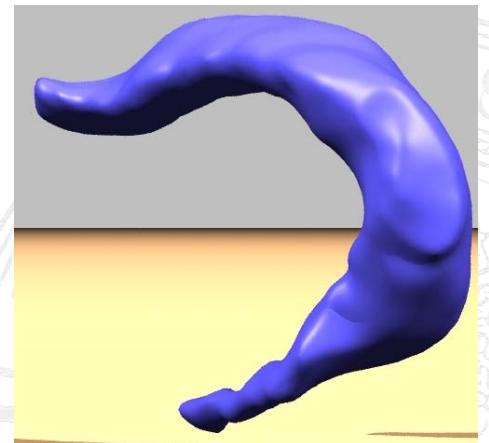
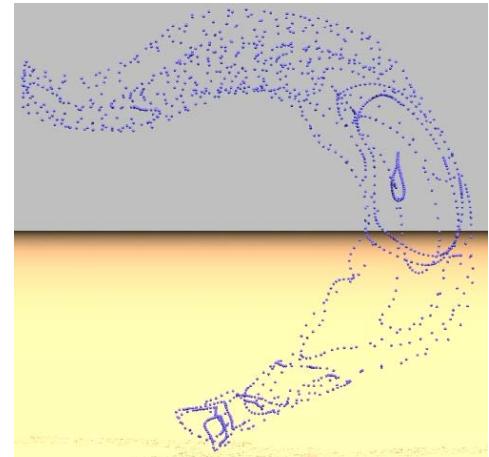
- Surfaces from Unorganized Points
- Radial Basis Functions



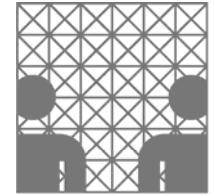
Implicit Function Fitting



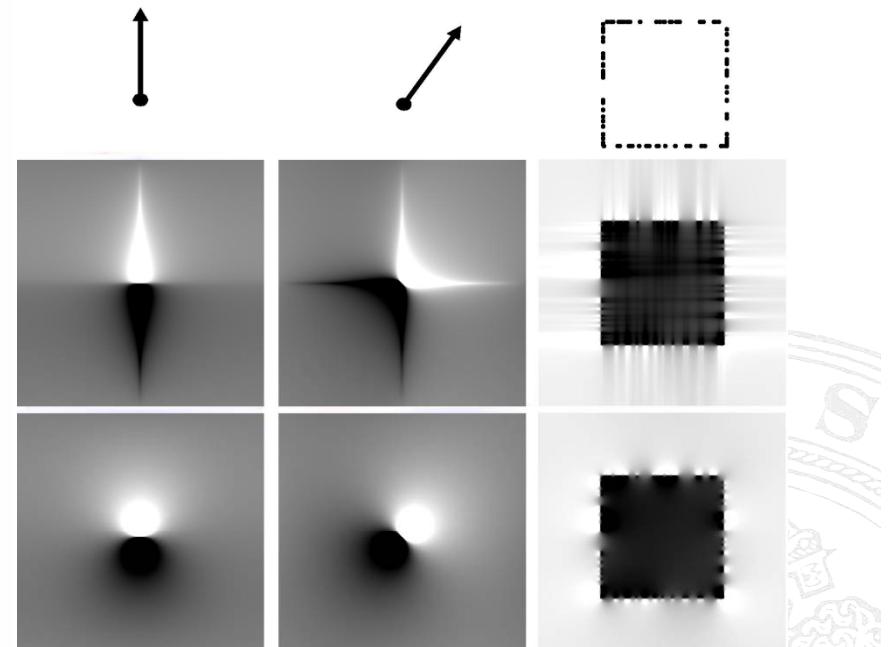
- Surfaces from Unorganized Points
- Radial Basis Functions
- Level Sets

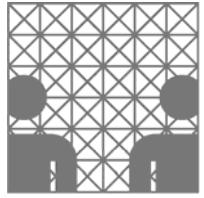


Implicit Function Fitting



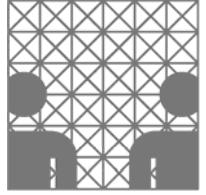
- Surfaces from Unorganized Points
- Radial Basis Functions
- Level Sets
- FFT-Based Reconstruction





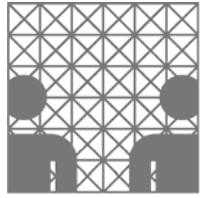
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